

**Industrial Organization and Public Policy
Economics 640**

Solutions to Midterm Examination

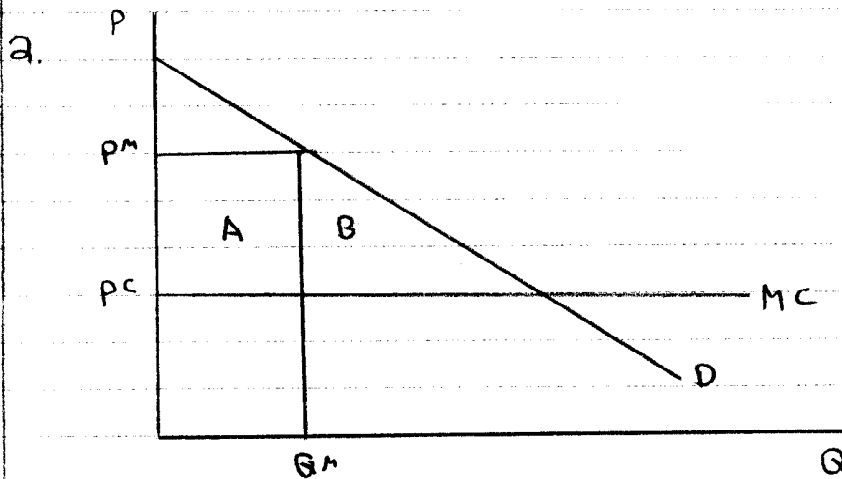
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I. Short Answer

1. Competitive Outcome : $P^c = MC = 4$

Monopoly Outcome : $MR = MC \Rightarrow 6 - 8Q = 4$
 $\Rightarrow 6 - 4 = 8Q$
 $\frac{2}{4} = \frac{1}{2}Q = Q^M$

Monopoly Price : $P(Q^M) = 6 - 4\left(\frac{3}{4} - \frac{1}{2}Q\right) = 6 - 3 + 2Q < 4 = P^c$
 $3 + 2Q < 4$
 $2Q < 1$
 $Q < \frac{1}{2}$



Posner suggested that the "transfer" A could be dissipated in the course of rent-seeking to become a monopolist. Hence, total social costs of monopoly could range as high as $A + B$ (traditional DWL). A is equal to monopoly profits. With linear demand and cost, $DWL = \frac{1}{2}$ monopoly profit.

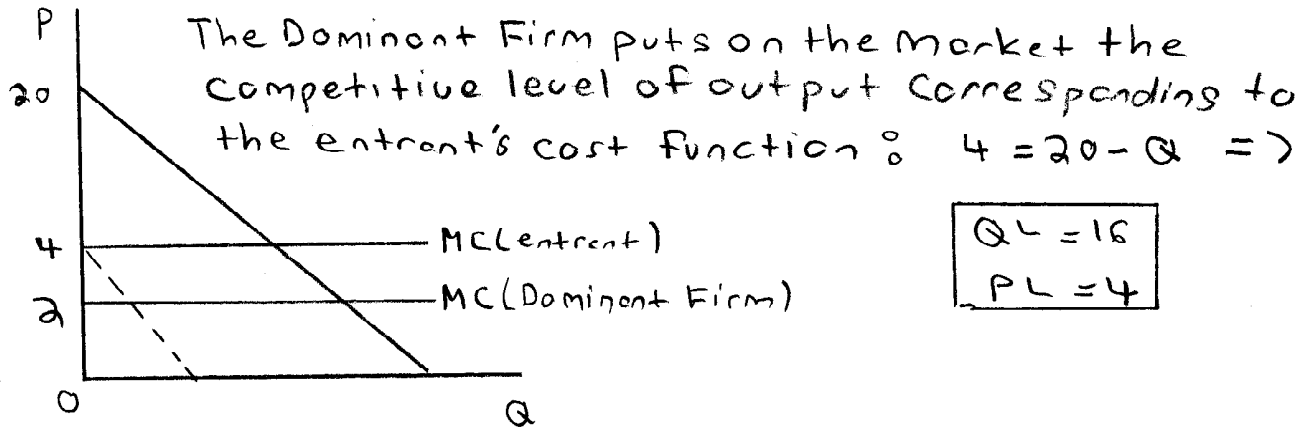
$$B = 100 = \frac{1}{2} \text{ monopoly profit} \Rightarrow A = 200$$

$$A = 200$$

$$B = 100$$

Total Social Costs = 300

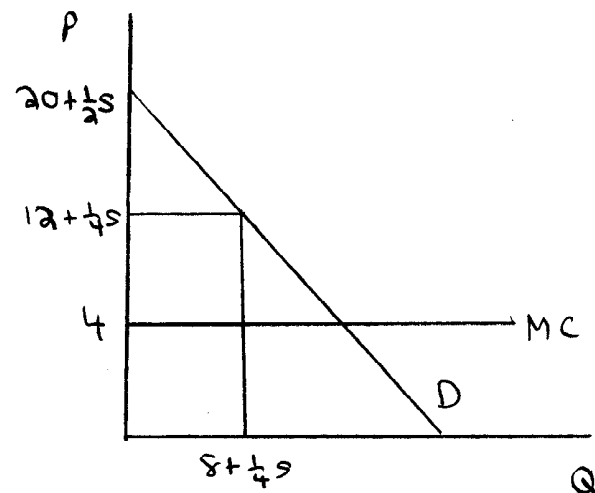
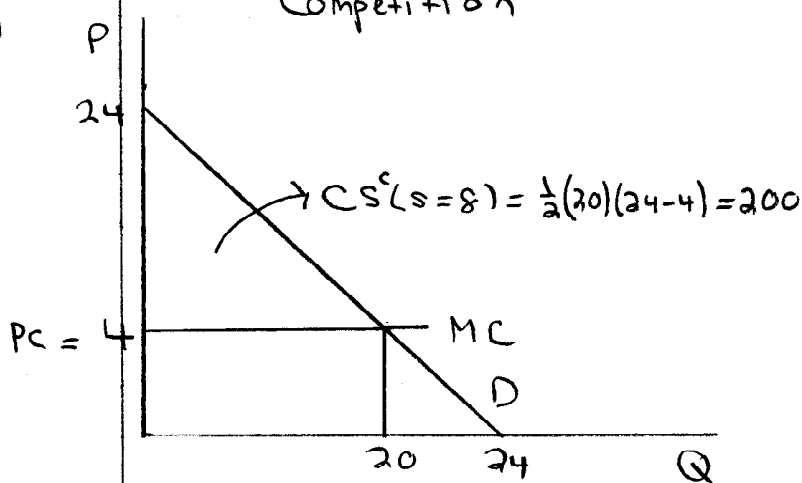
$$3. P(Q) = 20 - Q. \quad C(Q) = 2Q, \quad C(q) = 4Q$$



$$4. P = 20 - 1Q + \frac{1}{2}s \quad C(Q) = 4Q$$

$$\text{With } s = 8, P = 24 - 1Q = 4 = MC = Q^c = 20, P^c = 20$$

Competition



Under monopoly, $MR = MC \Rightarrow 20 + \frac{1}{2}s - 2Q = 4 \Rightarrow Q^M = 8 + \frac{1}{4}s$
 The corresponding monopoly price is given by P^M

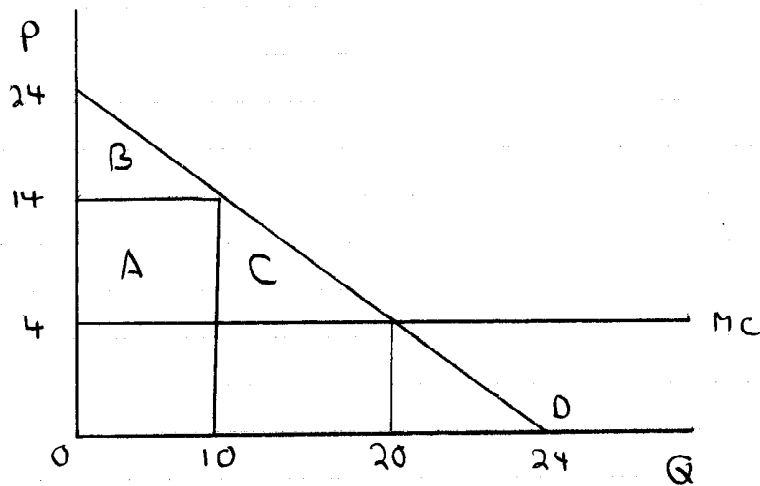
$$P^M = 20 - (8 + \frac{1}{4}s) + \frac{1}{2}s = 12 + \frac{1}{4}s$$

$$CS^M(s) = \frac{1}{2}(8 + \frac{1}{4}s)(20 + \frac{1}{2}s - 12 - \frac{1}{4}s) = \frac{1}{2}(8 + \frac{1}{4}s)^2 \geq 200$$

$$\Rightarrow 8 + \frac{1}{4}s \geq 20 \Rightarrow \frac{1}{4}s \geq 12 \Rightarrow \boxed{s \geq 48}$$

Note that at $s = 48$, $Q^M = 20 = Q^c$ When $s = 8$.

5. $P(Q) = 24 - Q$ $C(Q) = 4Q$



Monopoly Price: $24 - 2Q = 4 \Rightarrow Q^M = 10$
 $P(Q^M) = 14$

Monopoly Profits: $\pi^M = Q^M (P^M - MC) = 10(14 - 4) = 100$

Consumers would have to bribe the monopolist with its monopoly level of profits = A.

Consumers enjoy net CS of B + C

Hence $PS = A$
 $CS = B + C$

$W = A + B + C = \frac{1}{2}(20)(24 - 4) = 200$

6. $Q = 20 - 2P \Rightarrow P = 10 - \frac{1}{2}Q$

This is a linear demand function. The revenue-maximizing price occurs at the midpoint of the linear demand function. This corresponds to $P = 5$ and $Q = 10$

$\epsilon = \frac{dQ}{dP} \cdot \frac{P}{Q} = (-2) \frac{5}{10} = -1$

II Problems

$W = \alpha CS + (1-\alpha) PS \quad \alpha \in [0,1]$

$Q = 32 - 2P \Rightarrow P = 16 - \frac{1}{2} Q$

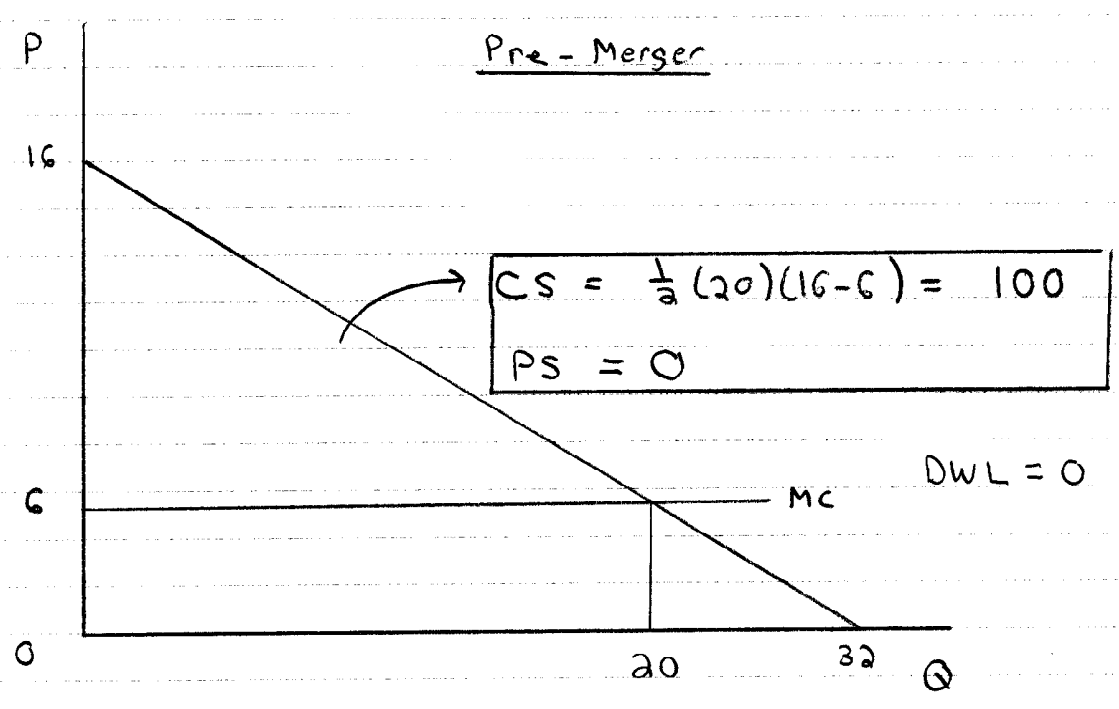
$C(Q) = 6Q \quad \text{Pre-Merger}; \quad C(Q) = 4Q \quad \text{Post-Merger}$

a) Pre-Merger Competitive Outcome

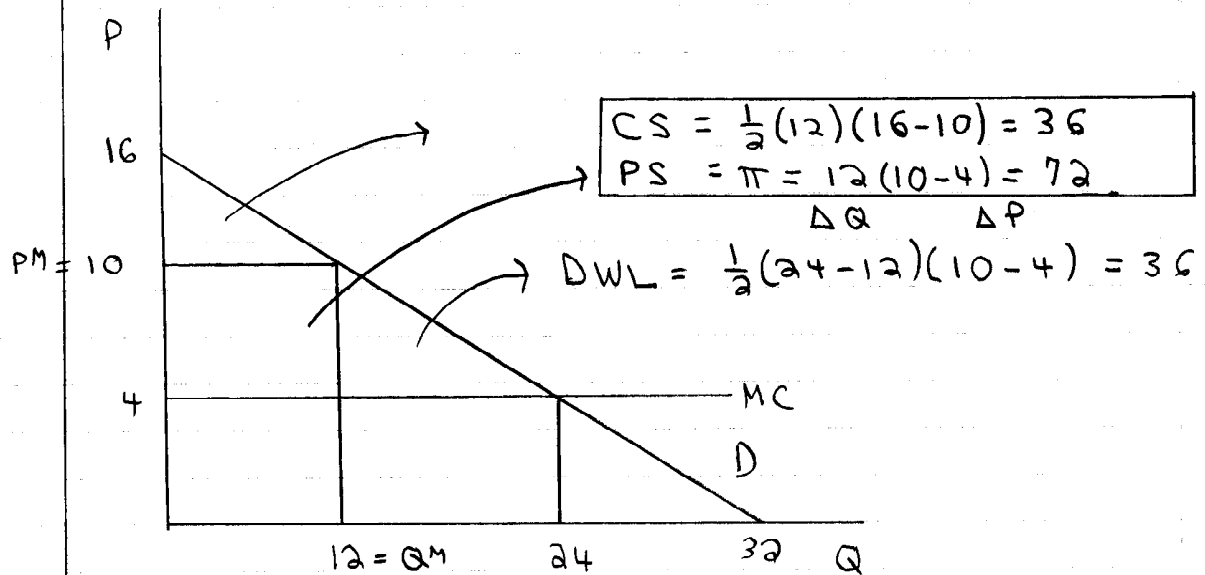
(1) $P^c = MC = 6; \quad Q(6) = 20$

Post-Merger Monopoly Outcome

(2) $\overbrace{16 - Q}^{MR} = \underbrace{4}_{MC} \Rightarrow Q^M = 12, \quad P^M = 10$



Post-Merger



Alternatively, $DWL = W^C - W^M = 100\alpha + 0 - 36\alpha - 72(1-\alpha)$
 $= 136\alpha - 72$

b) Pre-Merger $DWL = 0$; Post-Merger $DWL = 36$

c) $W = \alpha CS + (1-\alpha) PS$

$$\Delta W = [\alpha(36) + (1-\alpha)72] - [\alpha(100) + (1-\alpha)0] < 0$$

$$36\alpha + 72 - 72\alpha - 100\alpha < 0$$

$$72 - 136\alpha < 0$$

$$\Rightarrow \alpha > \frac{72}{136}$$

$$\Rightarrow \alpha > 0.5294$$

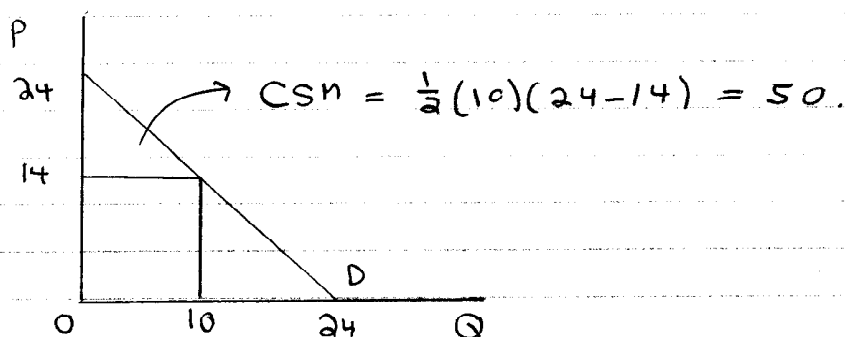
d) No. Democratic administrations tend to place more weight on CS than on PS and this implies that $\alpha > 0.5$. The analysis reveals that the merger is welfare diminishing for all values of $\alpha > 0.5294$. Hence, it is unlikely that the Obama administration would look favorably upon this merger.

2. $P = 24 - t(q + Q)$. $C(Q) = 4Q$ - Dominant Firm's Cost Function. $C(q) = e + 4q$ - Entrant's Cost Function.

a) Monopoly Outcome For Dominant Firm, Set $q = 0$

(1) $P = 24 - Q$. Set $MR = MC$

$$(2) \underbrace{24 - 2Q}_{MR} = \underbrace{4}_{MC} \Rightarrow Q^M = 10 \Rightarrow P^M = 14$$



b) $P(Q) = 24 - q - Q$ or $P(Q) = (24 - Q) - q$.

The fringe acts as a monopolist on that portion of the market demand curve remaining after the dominant firm has placed Q amount of output on the market.

(3) $MR(q) = 24 - Q - 2q = 4 = MC$ Solve for q ,

$$(4) 24 - 4 - Q = 2q \Rightarrow q = 10 - \frac{1}{2}Q$$

c) The fringe profit function is given by

(5) $\pi^f = (P - MC)q - e$. Substitute for P and MC

$$(6) \pi^f = (24 - q - Q - 4)q - e$$

$$(7) \pi^f = (20 - q - Q)q - e$$

Substitute in for q ,

$$(8) \pi^f = [20 - (10 - \frac{1}{2}Q) - Q][10 - \frac{1}{2}Q] - e$$

$$(9) \pi^f = [10 - \frac{1}{2}Q]^2 - e$$

Set $\pi^f = 0$ and solve for Q

$$(10) [10 - \frac{1}{2}Q]^2 = e$$

$$(11) 10 - \frac{1}{2}Q = \sqrt{e}$$

$$(12) 10 - \sqrt{e} = \frac{1}{2}Q$$

$$(13) Q^L = 20 - 2\sqrt{e}$$

When $e = 0$, $Q^L = 20$ and $P^L = 4 = MC$

Hence, when there are no sunk costs of entry ($e = 0$), the dominant firm must put the "competitive" level of output on the market and charge the "competitive" price in order to keep the fringe firm out.

d) For $Q^L = Q^M$, it follows that

$$(14) 10 = 20 - 2\sqrt{e} \Rightarrow 2\sqrt{e} = 10$$

$$\Rightarrow e = 25$$

Note that $\pi^f = [10 - \frac{1}{2}(10)]^2 - 25 = 0$.

Economic Intuition: When the sunk costs of entry are sufficiently high (i.e., $e \geq 25$), the dominant firm can act like a monopolist. In this case, the fringe firm exerts no discipline on the behavior of the dominant firm.

3. Essay

There is no single "correct" answer to this essay. Grading was based on:

- (1) Use of references/literature to support the fundamental premises of your discussion.
- (2) The Economic logic employed in your discussion.
- (3) Whether your arguments were well-reasoned and flow logically from your basic premises.
- (4) The objectivity and coherence of your writing.
- (5) Discussion of costs/benefits of antitrust pursuits and principles that derive therefrom.
- (6) Distinction between Consumers' Surplus and Economic Welfare.

Essential Points.

- 1) Differentiate Between CS and W
- 2) Williamson Analysis: "Rectangles Dominate Triangles" Theorem
- 3) $\hat{W} = \alpha CS + (1 - \alpha) PS$, $\alpha \in [0, 1]$
- 4) Chicago / Harvard - SCP. low/high α , respectively
- 5) Senator Sherman's Focus on CS - increase in price was concern? What about innovation and "creative destruction"?
- 6) Cost Savings Realized By Firm - Higher Prices Borne by Consumers. Related Back to 2) and 3)
- 7) Readings: Carlton, Schumpeter, Antitrust Modernization Commission Report, Baker, Crandall and Winston
- 8) Should antitrust be concerned solely with efficiencies, regardless of distribution issues - why, why not? arguments