Advertising and Labor Market Matching: 
A Tour Through the Times*

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Abstract
Surveying newspapers spanning four centuries, we identify four employment-related advertising eras (neither workers nor firms posted ads, mostly workers posted, mostly firms posted, both parties posted). Modeling the job matching process as a strategic coordination game, we identify four equilibria that correspond to these eras. We suggest three complementary explanations for transitions across eras: an increase over time in firm size and the labor force, an increase in worker mobility and a reduction in search frictions, and a decrease over time in the workers’ relative value of labor versus unemployment. A discontinuous welfare function has policy implications for job matching.

Keywords: labor market matching, recruitment, job search, newspaper advertising

JEL Classification: J23, J63, M51, N3

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1 Introduction

The matching of job seekers to employers is a fundamental subject in labor economics that also has implications for macroeconomic discussions of unemployment. Furthermore, understanding the impacts of many labor market and macroeconomic policies hinges on what we know about the job matching process. The matching framework (e.g. Pissarides 2000, Mortensen and Pissarides 1999) posits a matching function that summarizes, in the aggregate, the outcomes of encounters between job seekers and recruiting employers. The matching function reflects the transaction costs and search frictions arising from imperfect information.\(^1\) To combat these frictions, both sides of the market can influence the matching function by making investments that improve information.\(^2\) But which side of the market should make those investments? How do the investments made by one side of the market influence those made by the other side? What are the implications of having the investments occur on one side of the market versus the other? Answering such questions requires shining light “under the hood” of the matching function, as we do in this study.

Although search-related investments are implicit in the matching function, they are rarely the primary objects of research interest.\(^3\) Furthermore, when search strategies are in the spotlight the focus is typically on the behavior of only one side of the labor market, and strategic interactions between the job seeker and the employer are ignored.\(^4\) Our goal is to learn about the job matching process by investigating how advertising behaviors of employers and job seekers have changed historically and by developing an explanatory theoretical framework that accounts for strategic interactions in these investments.

We start by reading the employment-related ads in newspapers – lots of them, spanning over four hundred years, multiple languages, and locations as diverse as Austria, England, Ireland, Scotland, the United States and its original

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\(^1\)See Petrongolo and Pissarides (2001) for a survey of the matching function.

\(^2\)For example, job seekers can learn about job vacancies by exploiting personal networks of friends and relatives, reading job ads online or in the newspaper, contacting state or community employment agencies, and attending university career fairs, whereas employers can learn about prospective hires by soliciting the referrals of current employees and friends, posting “help wanted” signs or ads online or in newspapers, consulting unions or state employment agencies, or attending university career fairs.

\(^3\)The literature on employer recruitment strategies, for example, remains a backwater. A quote from Granovetter’s seminal work in the early 1970s still rings true today: “While people are finding jobs, employers are finding people to fill them, and their behaviors, strategies, and purposes play a central but often neglected role in the process of matching people to jobs” (Granovetter 1995).

\(^4\)For example, although employer recruitment strategies were treated as endogenous choices in DeVaro (2008), job seeker search strategies were not modeled in that analysis.
colonies, Jamaica, Barbados, India, and seventeenth-century Strasbourg. Based on this reading, we identify four eras in advertising history. Until the 19th century, newspaper ads posted by either employers or job seekers were rare, and we call this the “Pre-Ad era”. When ads began to appear regularly starting in the nineteenth century, those posted by job seekers tended to dominate the market, and we call this the “Early era”. For example, the October 24, 1871 edition of The New York Times contained 138 employment-related ads, only 8 of which were employer-posted “Help Wanted” ads, featuring a dozen positions for cooks, canvassers, coachmen, seamstresses, chambermaids, waitresses, laundresses, and an opportunity in a life insurance office. The remaining 130 were “Situations Wanted” ads, divided into a section for females and another for males. A dramatic reversal then occurred, such that by the late twentieth century nearly all ads were posted by employers, and we call this the “Modern era”. For example, the October 24, 1971 edition of The New York Times contained thousands of ads, and we estimate that about 96 percent of them were posted by employers. So less than 6 percent of the ads on October 24, 1871 were employer posted, versus 96 percent in the same newspaper, on the same date, a century later. Finally, the advent of the internet allowed electronic ads to be posted at low cost, resulting in today’s significant volume of online posting by both sides of the labor market. We call this the “Internet era”. After documenting these intriguing observations, we develop a theoretical model that can explain all of them. The model exhibits equilibria corresponding to each of the four eras and suggests several complementary explanations for the historical evolution across the equilibria.

Although we focus on the labor market, the question of which side of the market should undertake search-related investments is quite general, and for that reason the theory we develop could apply to other matching markets (e.g. the rental housing market, in which both sides of the market regularly post

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5Sunday, October 24, 1971 can be considered a randomly selected date, except to the one of us who was born on it! Since the ads on that date are so numerous, we approximated the fraction posted by employers. The main collection of ads spans all of Section 9 (pages 1-34). Each column of text on a page contains dozens of individual ads, and there are 303 columns of ads in total in Section 9. Fewer than 12 of those columns contain “situations wanted” ads posted by job seekers. These numbers form the basis for our estimate of 96 percent, though in fact the fraction of total ads placed by employers was even larger, since there are some other locations in the newspaper containing scattered employer-posted ads. For example, ads can be found in the business section between pages 17 and 30, and ads for teachers can be found on pages 12 and 13 of Section 4.

6It is now common for job seekers to post ads (typically in the form of résumés on sites like monster.com and professional networking sites like LinkedIn) as well as employers.
on websites such as craigslist). The following example illustrates the generality of the investment problem. Two blindfolded individuals are randomly located at different positions on an empty playing field. Their objective is to find each other to collect a shared prize, and the rules prevent them from communicating. Each is free to remove his blindfold at a cost. If neither chooses to do so, they might never find each other. If one of them removes the blindfold, they should find each other easily, and a positive externality is created by the party who invests. And given that one of them removes the blindfold, there is little benefit to the other of removing the blindfold, which creates the potential for free riding. There are four possible outcomes: both blindfolds remain on, both are removed, or two distinct ways in which only one is removed. But which outcome(s) prevail, and why? In the special case of the labor market, our review of the newspaper evidence reveals that the four “blindfold outcomes” are reminiscent of the four advertising eras that have occurred historically.

Our model is a strategic game of coordination involving $N$ homogeneous job seekers and a single firm that could employ up to $m$ workers, where $1 \leq m \leq N$.\footnote{Our assumption of homogeneous preferences differs from the matching literature, originating with Gale and Shapley (1962) and subsequently developed by Roth and others, in which heterogeneity of preferences is key. The notion of match stability is therefore irrelevant in our model, and our welfare analysis has a somewhat different flavor. In the matching literature, social welfare hinges on the exact configuration of matches, whereas in our model one match is as good as any other, and the welfare analysis hinges on the likelihood that a match occurs at all and on who pays the investment costs to increase the likelihood of a match.}

In the first of three stages, workers and the firm simultaneously decide whether to post an ad (at a cost). Matches occur in the second stage, with match probabilities influenced by who posts in the first stage. Hiring occurs in stage 3, when payoffs accrue to both sides of the labor market in the form of wages and profits.

In the simplest case of a two-player game with one worker and one firm, the model exhibits the following four pure-strategy equilibria, analogous to the four “blindfold outcomes” from our example: neither side posts (NP), both sides post (BP), only the firm posts (FP), or only the workers post (WP). These equilibria match or approximate the behaviors we have observed in the historical record. The Pre-Ad era was characterized by essentially no posting by either side of the market and is well described by the NP equilibrium. Advertising in the Early era was dominated by job seekers, although a small fraction of employer-posted ads also appeared, and there are two ways to understand this era in the context of our model. One possibility is that equilibrium BP applies. Another possibility is that equilibria FP and WP both coexisted during this era, implying that
the structure of the game resembles that of battle of the sexes. The observed behavior could then be explained in two ways: either some people failed to coordinate on the same equilibrium or some occupations and industries played equilibrium FP and others played WP. The Modern era in which advertising was dominated by employers is well described by the FP equilibrium. The current Internet era in which both sides regularly post online ads is well described by the BP equilibrium.

We attribute the transition from the Pre-Ad to the Early era to decreases in the costs of posting ads that occurred because of increasing literacy rates, which in turn were fueled by the technological progress that accompanied the Industrial Revolution and by the growth of public school systems. Similarly, we attribute the transition from the Modern to the Internet era to decreases in the costs of posting ads that occurred because of the Internet Revolution. We provide three complementary explanations for the transition from the Early to the Modern era: growth in both firm size and the labor force over time, an increase in job mobility and a reduction in search frictions over time, and an increase over time in the jobseekers’ outside option of unemployment, due to the emergence of social insurance programs in the twentieth century. We elaborate on all of these explanations after developing the theoretical model.

This work relates to a literature on recruitment that dates back at least as far as Malm (1954, 1955). The role of employer recruitment strategies as an information generating device was first explored in Rees (1966). Since Rees and Shultz (1970), much of the literature on recruitment and worker job search has focused on the role of informal methods (such as soliciting referrals from current employees, friends, or relatives) in labor market matching. For example, Pinkston (2012) and Simon and Warner (1992) conducted empirical tests of the hypothesis that informal referrals generate more precise information about job applicants than other recruitment methods. DeVaro (2005) analyzed how a variety of recruitment methods relate to vacancy durations and starting wages. The recruitment methods considered included informal methods and a variety of

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8The crucial role that information plays in the labor market has been appreciated since Stigler (1962).

9See also Loury (2006), Castilla (2005), Kugler (2003), Menken and Winfield (1998), Mortensen and Vishwanath (1994), Montgomery (1991), Blau and Robins (1990), and Holzer (1987,1988). While the idea that informally recruited new hires could yield better matches became popular following Rees (1966) and Rees and Shultz (1970) it had also been noted earlier. For example, Reynolds (1951) discussed a retention benefit deriving from workforce congeniality and residential co-location.

10See also Bencenč (2009), Barron et al. (1997), Gorter et al. (1996), van Ours and Ridder (1992), and Roper (1988).
formal methods (such as newspaper advertising), though consistent with most of the literature all of the recruiting methods were treated as exogenous. In a related analysis, DeVaro (2008) estimated a dynamic structural model to identify the effects of recruiting channels on starting wages and vacancy duration, treating recruitment methods as endogenous. The key tradeoff in that model is that informal methods (consistent with the arguments in Rees and Shultz and the subsequent literature) are expected to yield higher-quality matches, whereas formal methods such as newspaper advertising generate a larger applicant pool from which the employer can be more selective. Our focus is on formal methods (and in particular advertising) rather than informal methods.

The work also relates to a growing literature on two-sided markets (or networks). These markets involve a “platform” that facilitates transactions between two “end users”, getting both parties “on board”. For example, a credit card platform connects buyers and vendors; the credit card network can attract customers if stores accept its card, but stores will only accept the card if there are many customers. In our context, the platform is the newspaper, the end users are job seekers and employers, and “getting both sides on board” means commencing an employment relationship. This corresponds to the rough definition of a two-sided market offered in Rochet and Tirole (2006), which cited the newspaper as an example that competes for advertisers as well as “eyeballs”. The theory relates to an older literature on network externalities (originating with Katz and Shapiro 1985 and 1986, and Farrell and Saloner 1985 and 1986) by assuming that there are non-internalized externalities among end users. For example, if a store accepts a credit card, it creates a positive externality for customers who want to use that card. In our model, the firm creates positive externalities for the workers by posting ads, and workers create positive externalities for the firm and negative externalities for each other by posting ads.

Our model delivers important and unexpected welfare implications. For example, policies that hinder job mobility and increase search frictions can actually enhance welfare, if they sufficiently weaken the incentive of one side of the market to free ride on the investments of the other; when both sides of the market are induced to post ads, the positive externalities enjoyed by the workers (as a result of the firm posting) and by the firm (as a result of the workers posting) may outweigh the negative externalities suffered by workers (as a result

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11 See, for example, Rochet and Tirole (2003, 2006), Parker and Van Alstyne (2005), Rysman (2009), Weyl (2010), and Eisenmann, Parker, and Van Alstyne (2011).
of their fellow job seekers posting). Similarly, small labor market interventions to increase job mobility and reduce search frictions can lead to large reductions in welfare that arise when one side of the labor market is induced to free ride on the investments made by the other side. An implication of these arguments is that policies aimed at reducing the costs of posting and reading ads may be superior to those designed to increase job mobility and reduce search frictions. More generally, changes in the model parameters (from policy interventions or for other reasons) change welfare in two ways. First, conditional on a specific equilibrium being played, changes in the model parameters affect workers’ and firms’ payoff in this equilibrium. Second, changes in the model parameters may induce workers and firms to behave differently, i.e. to switch to a different equilibrium. Because of this latter effect, a small change in one of the model parameters may have a large effect on welfare (i.e. the welfare function is discontinuous). This gives rise to a range of policy implications such as those just described.

2 Employment-related advertising: a tour through the Times

Employment-related advertising has surely existed, in some form, for as long as there have been labor markets. One longstanding method of advertising that is still used is physically posting a visible indicator, such as a “Help Wanted” sign, in a public area or storefront window. This method is simple, effective, and cheap, though a downside is that people must attend the physical location to notice the ad, and they have no way of knowing in advance whether they will find an ad if they visit a particular location.\footnote{This method is also used by the other side of the labor market. For example, in some California cities job seekers congregate in a collectively known location that is frequented by roofing contractors (e.g., a Home Depot). When the contractors arrive at the store to purchase the materials needed for that day’s work, they hire these day laborers on the spot to help with the roofing projects for that day. Thus, the job seekers advertise their availability by “posting” their own physical presence at a given location.} Today, the problem of reaching a large audience without requiring readers to travel to a physical location has been solved by the internet, and ads increasingly appear on job matching sites like monster.com, or on professional networking sites like LinkedIn. The electronic ad, however, is a recent phenomenon. Between these two extremes of the internet and physically posted ads lies the newspaper, which emerged in the
early seventeenth century.\textsuperscript{13} For centuries preceding the advent of the internet, the newspaper offered both sides of the labor market their best option to reach a widely dispersed audience at a reasonable cost.\textsuperscript{14}

The advent of the newspaper induced a massive drop in the cost of disseminating information quickly to a large audience spread over a wide geographic area, so it is natural to expect that the newspaper would have evolved rapidly into an important vehicle for labor market matching. But our investigation suggests that employment-related newspaper advertising did not become a regular phenomenon until the nineteenth century. To establish this fact, we read many newspapers, printed in both English and German, spanning many geographic areas, and dating back to 1609. Although we provide a summary in Table 1, our review was more exhaustive than what we have displayed in the table.\textsuperscript{15} We see that prior to the start of the Industrial Revolution around 1760, employment-related advertising by either side of the labor market was virtually non-existent. We found no ads in the newspapers we read from the seventeenth century. The oldest ad we found was posted by a job seeker named Thomas Ward in \textit{The Weekly Jamaica Courant} on July 30, 1718. For the remainder of the eighteenth century, ads appeared only sporadically, sometimes posted by job seekers and sometimes by employers. Since ads were extremely rare during the period covered in Table 1, we refer to this as the “Pre-Ad” era. In the context of the theoretical model we develop in the next section, the Pre-Ad era is best described by the NP equilibrium in which neither employers nor job seekers post ads.

To document what happened during the period of regular posting that emerged in the nineteenth century, we provide a tour through the histories of two celebrated and currently circulating newspapers, namely \textit{The Times} of London and of New York.\textsuperscript{16} We begin with the London newspaper. Table 2

\begin{table}
\caption{Summary of Employment-Related Advertising in 17th-Century Newspapers}
\begin{tabular}{|c|c|}
\hline
Newspaper & Date \tabularnewline
\hline
\textit{The Weekly Jamaica Courant} & 1609 \tabularnewline
\hline
\textit{Relation aller Fürnemmen und gedenckwürdigen Historien} & 1605 \tabularnewline
\hline
\textit{The Maryland Gazette} & 1727 \tabularnewline
\hline
\end{tabular}
\end{table}

\textsuperscript{13}As noted in Weber (2006), the first newspaper appears to be \textit{Relation aller Fürnemmen und gedenckwürdigen Historien}, which was founded in Strasbourg in 1605 and published in German.

\textsuperscript{14}Televised job ads have never been very popular. Even though they can reach a large audience immediately and without requiring consumers to attend a particular location, the cost of air time is high. Furthermore, a newspaper can be read at one’s leisure, and the reader knows where in the newspaper to find all of the ads in one place. In contrast, television ads appear individually and sporadically and must be consumed contemporaneously.

\textsuperscript{15}We did a particularly thorough investigation of \textit{The Maryland Gazette}, starting with the 1745 issues that were readily available to us on microfilm. Founded in 1727, \textit{The Gazette} is one of the oldest newspapers in the United States. Perusing many issues, we found no employment-related ads from 1745 through the early nineteenth century.

\textsuperscript{16}We selected these newspapers because of their long histories, international reputations and stature, and diverse geographic locations. According to Wikipedia, the printed version
displays a tour through *The Times*, from 1785 through 1991. We examined the October 24 editions at intervals of a decade, stopping in 1991 since that was the last year for which we had convenient microfilm access and because that date was sufficiently late for our purposes.\(^1\) If October 24 fell on a Sunday during a year in which *The Times* did not have a Sunday edition, we used the edition from an adjacent day. Our objective was to see whether employment-related ads were posted mostly by employers, mostly by job seekers, or regularly by both sides of the labor market. In most years we provide an exact count of ads, though we provide approximations for years in which the quantity of ads is overwhelmingly large or in which counting is otherwise inconvenient. As seen in the first three rows of Table 2, the absence of ads in 1785 and 1795 and the paucity of ads in 1805 are consistent with the conclusion we drew from Table 1. Table 2 reveals that employment-related ads were not a regular phenomenon until the nineteenth century was well underway.

The next several rows of Table 2 reveal that when employment-related ads became a regular fixture in the newspaper, they were dominated by job seekers rather than by employers. The year 1845 was an exception given that the fraction of ads posted by employers reached nearly 43 percent, but even then the fraction was well under half. By 1855 that number dropped back down to 17.5 and remained under 30 percent for the rest of the century. Our impression is that 1845 was anomalous and driven by the railway boom witnessed by London in the 1840s. A lot happened on the railway front in London between the years of 1835 and 1845. The Euston terminus was built at the end of the line from Birmingham, bringing long distance railroad travel to London in 1837. Two other major terminals followed, with Paddington opening in 1838 and Fenchurch Street opening in 1841. Permission was also sought from Parliament for 19 new railway lines in London. The early 1840s also witnessed an increase in government regulation of the railways, such as the Railway Regulation Acts of

\(^\text{17}\) We also considered a number of other randomly selected dates to assure ourselves that there is nothing special about October 24.
1840 and 1844. Many of the ads in the 1845 newspaper suggest a considerable and immediate demand for labor on the railways, often at high wages. The following ads from that edition - all of which appear in a single column on the front page of the newspaper - are representative:

TO SURVEYORS AND LEVELLERS. – WANTED, from 20 to 30 first-rate HANDS, to whom a liberal payment will be given. Apply, by letter post paid, to C.E., care of J.E. McCabe, surveyor and lithographer, 35 Castle Street, Holborn [illegible].

TO SURVEYORS AND LEVELLERS. – WANTED, immediately, a PERSON to teach surveying and levelling, one who has the proper instruments will be preferred. Address, post paid, to X, Y, Z, at Mr. Starling’s, bookseller, Islington.

TO RAILWAY SURVEYORS. – WANTED, immediately, two or three good RAILWAY SURVEYORS. Liberal terms will be given. Address by letter to O.M., Railway Mail Office, Coleman Street, stating references, &c.

Taken together, Tables 1 and 2 reveal that prior to the Industrial Revolution a “Pre-Ad” era prevailed with little or no posting by either side of the market, and near the end of the Industrial Revolution a new era emerged in which ads were regularly posted and were more commonly placed by job seekers than by employers (the exception of 1845 notwithstanding). We refer to this period, which lasted throughout the nineteenth century, as the “Early era”. From 1815 to 1905 (and excluding the 1845 anomaly) the average of the entries in Table 2 is 20 percent, so that 4 out of every 5 ads in the newspaper over the course of nearly a century were placed by job seekers rather than by employers. For the period preceding the railway boom, i.e. 1815 to 1835, the average entry in Table 2 suggests that about 88 percent of ads were posted by job seekers. Our model exhibits a BP equilibrium in which both sides of the market post ads. Another possible interpretation of the Early era is that it reflects a blend of the FP and WP equilibria, with either of these equilibria applying to certain occupations or industries.

Table 2 reveals that the fraction of ads posted by employers jumped from less than 23 percent in 1905 to more than 55 percent in 1915. This appears to be the start of the “Modern era” in which employment-related ads were dominated by employers rather than by job seekers. By 1975 and 1985 the fraction of ads posted by employers exceeded 90 percent, and by the early 1990s the ads were too numerous to count and were posted almost entirely by employers. This situation is well described by the FP equilibrium from our model, in which all
ads are employer posted.

The Modern era ended with the advent of the internet at the end of the twentieth century, which revolutionized employment-related advertising. By the early twenty-first century both employers and job seekers were regularly posting online ads to capitalize on the reduced advertising costs and widened audiences that electronic distribution allows.\textsuperscript{18} This era is characterized by the strong resurgence of ads posted by job seekers. In October 2013, on the homepage of monster.com, the very first link was “Resumes” which allows the user to post a résumé, and the second link was “Jobs” which allows the user to search a database of employment opportunities. This is poignantly reminiscent of how, throughout the Early era, the “Situations Wanted” ads were placed first in the newspaper, followed by a smaller “Help Wanted” section. This fourth and ongoing “Internet era” is well described by our model’s BP equilibrium.

Figure 1 provides a visual representation of the transition from the Early era to the Modern era by plotting the numbers in Table 2. We begin the plot in 1815 because in 1785 and 1795 there were no ads posted by either side, and in 1805 there were only three ads, which we see as an extension of the Pre-Ad era depicted in Table 1. Figure 1 starts with virtually none of the ads posted by employers and ends with all of the ads posted by employers. This striking trend is not unique to London. The results of a tour through The New York Times appear in Table 3 and Figure 2. We considered the October 24 edition, by decade, from 1851 to 2011.\textsuperscript{19} Figure 2 bears a striking resemblance to Figure 1. Clearly, throughout the latter half of the nineteenth century The New York Times was dominated by ads posted by job seekers, whereas by 1991 this situation had flipped, and nearly all ads were posted by employers. As seen in the first few rows of Table 3, in the years 1861, 1871, and 1881 the fraction of employer-posted ads was less than 5 percent. In contrast, by 1991, as was true in London, virtually all ads were employer posted, a situation which is well

\textsuperscript{18}See Brenčič (2013) for empirical evidence on the number of jobs and the numbers of CVs posted on various online job sites from 2002 to 2012. For example, in 2012 the 100 most popular cites featured about 208,000 jobs and about 2 millions CVs.

Kuhn and Mansour (2011) found that internet job search continues to grow rapidly and that it is now effective and reduces unemployment durations by 25 percent, whereas earlier evidence in Kuhn and Skuterud (2004) and Kroft and Pope (2010) suggested that internet job search was largely ineffective. The increase in online job search has generated growing research interest in the nature of these activities. For example, in a pair of studies of online employer postings on job boards, Brenčič and Norris (2009, 2012) consider the content of online ads and the ways in which employers use these job boards.

\textsuperscript{19}No ads appeared in the 1851 issue, though by October 24 the newspaper had only existed for just over a month, so it might have required some time to establish itself.
captured by our FP equilibrium. The pattern of evidence from Figures 1 and 2 extends beyond London and New York. In fact, we first discovered it in The San Francisco Chronicle from 1865 to the present.

To summarize, we have identified four eras in advertising history. The Pre-Ad era, which prevailed through the seventeenth and eighteenth centuries and was brought to an end when the Industrial Revolution reached a climax, was characterized by little or no posting by either side of the labor market. The following Early era, which started in the latter part of the Industrial Revolution and extended to the early twentieth century, was characterized by regularly posted employment-related ads that were dominated by job seekers rather than by employers. The subsequent Modern era featured the decline and ultimately the near extinction of ads posted by job seekers. The fourth and ongoing Internet era coincided with the turn of the twenty-first century and was characterized by a resurgence of ads posted by job seekers, as both sides of the labor market regularly post ads online.

3 A model of advertising and labor market matching

We now develop a theoretical model to explain the evidence in the preceding section. For simplicity, we focus on the case of a single firm. The model has three stages. In stage 1, the firm, which seeks to hire up to \( m \) workers, and \( N \) workers simultaneously choose whether to post an ad. Posting an ad costs the firm \( c_p > 0 \). Since our newspaper evidence spans multiple centuries, illiteracy was widespread in the population of job seekers for much of the timespan we study. We therefore assume that there are two types of workers (literate and illiterate) that differ in their costs of posting ads. For literate workers these costs are \( c_p \), whereas for illiterate workers these costs are infinitely high. Thus, illiterate workers never post an ad, and we therefore focus on the decisions of literate workers. We denote the fraction of literate workers by \( \beta \in [0, 1] \) and define \( n := \beta N \) as the number of literate workers, where \( n \geq m \).

In stage 2, if the firm has posted an ad, a worker reads (or finds) the ad with probability \( \alpha \in (0, 1) \), in which case the worker contacts the firm. Similarly, if a worker has posted an ad, the firm reads the ad with probability \( \alpha \), in which case the firm contacts the worker. The parameter \( \alpha \) can be understood in different ways. First, an ad posted by one party may be overlooked by another party. For
example, the ad might be posted in one newspaper while the other party happens to read a different newspaper. Alternatively, one party’s ad might appear in the Tuesday edition of the newspaper, whereas the other party bought only the Wednesday edition. Second, α may account for impediments to mobility. For example, if a job seeker reads an ad that was posted by a firm, he might not respond to the ad if he faces mobility constraints or feels the firm is located too far away. In all these situations, a worker-firm match is not formed even though at least one side of the market posts. This possibility is captured by assuming α < 1.

If the firm contacts a worker or if a worker contacts the firm, and if the total number of contacts does not exceed m, the firm hires the worker in stage 3 and earns a (gross) payoff of \( u_F > 0 \) per worker, and each worker’s (gross) payoff from a match is \( \hat{u}_W > 0 \). If more than m contacts occurred, the firm hires each worker with the same probability. A worker’s reservation utility, i.e. the payoff that the worker receives if he is not hired by the firm, is denoted by \( u_0 \), where \( 0 \leq u_0 < \hat{u}_W \). Define \( u_W := \hat{u}_W - u_0 \). Worker i’s strategy is given by \( p_{Wi} \in \{0, 1\} \), where \( p_{Wi} = 1 \) means that worker i posts an ad. Similarly, the firm’s strategy is denoted by \( p_F \in \{0, 1\} \), where \( p_F = 1 \) means that the firm posts an ad. We focus on equilibria in pure strategies. If a party is indifferent between a lower and a higher action (for example, if worker i is indifferent between choosing \( p_{Wi} = 0 \) and \( p_{Wi} = 1 \)), we assume that the party always opts for the higher action (which in the example would be \( p_{Wi} = 1 \)).

We assume that job seekers are free agents, though in the earlier historical periods of our analysis slavery was common. For our analysis, the possibility of slavery does not alter anything fundamental. Like conventional labor, slave labor involves an exchange of money for labor services, and the labor market matching problem is similar for the two types of labor, with two main differences. First, in the context of slavery the payment goes to the worker’s current owner rather than to the worker, but from the firm’s standpoint it does not really matter who gets the payment. Second, and more importantly, slavery introduces a non-synchronization in revenues and costs in that all wage payments are front loaded in a lump sum payment in exchange for a future stream of “free” labor services. This non-synchronization shifts risk onto the employer, which is

\[ u_{iW} := \hat{u}_W - u_0 \].
presumably reflected in the price. A richer, dynamic model incorporating such nuances should leave our main results unchanged, and in any event our present static model with fixed wages permits an interpretation in which some of the job seekers are slaves. As for the data, newspaper ads from both sides of the slave labor market appear in the historical record, though they are not voluminous. Our reading suggests that most ads that concern slaves are posted by owners of runaway slaves with the hope of recovering lost property. This was especially so in the eighteenth-century issues of The Maryland Gazette we canvassed.

4 Model solution and comparison of equilibria

The random variable $X_i \in \{0, 1\}$ describes whether a contact between worker $i$ and the firm is made ($X_i = 1$). This happens either if the worker posts an ad that is read by the firm (event $A_i$) or if he reads an ad that is posted by the firm (event $B_i$). The probability of a contact is thus given by

$$q_i := P(X_i = 1) = P(A_i \lor B_i) = P(A_i) + P(B_i) - P(A_i \land B_i) = p_{W;i} + p_F \alpha - p_{W;i} p_F \alpha^2 = \alpha \cdot (p_{W;i} + p_F - p_{W;i} p_F \alpha).$$

Define $X := \sum_{i=1}^n X_i$ and $X_{-i} := \sum_{j \neq i} X_j$. Worker $i$ chooses $p_{W;i}$ to maximize

$$U_{W;i} = q_i \left( P(X_{-i} \leq m - 1) + \sum_{l=m}^{n-1} P(X_{-i} = l) \frac{m}{l+1} \right) u_W + u_0 - p_{W;i} c_p.$$

Notice that $X$ and $X_{-i}$ are distributed according to a Poisson binomial distribution. Hence, we observe $P(X = l) = \sum_{C \in F^l_i} \prod_{j \in C} q_j \prod_{k \in C^c} (1 - q_k)$ and $P(X_{-i} = l) = \sum_{C \in F^{n-1}_i} \prod_{j \in C} q_j \prod_{k \in C^c} (1 - q_k)$, where $F^l_i$ is the set of all subsets of $l$ integers that can be selected from $\{1, ..., n\}$. Notice further that $q_i$ is either equal to 0, $\alpha$ or $\alpha (2 - \alpha)$, i.e. there are just two different positive "success probabilities". In the following, we define $f(l; k, j) := P(X = l)$ when $k$ of the success probabilities are equal to $\alpha$ and $j$ of the success probabilities are equal to $\alpha (2 - \alpha)$. Note that $X$ is distributed according to the binomial distribution whenever $k$ or $j$ is equal to zero.
The firm chooses $p_F$ to maximize

$$U_F = (P(X \leq m) E[X | X \leq m] + P(X > m) m) \cdot u_F - p_F c_p$$

$$= \left( \sum_{l=1}^{m} l \cdot P(X = l) + m \sum_{l=m+1}^{n} P(X = l) \right) \cdot u_F - p_F c_p$$

$$= \left( \sum_{l=1}^{n} l \cdot P(X = l) - \sum_{l=m+1}^{n} (l-m) \cdot P(X = l) \right) \cdot u_F - p_F c_p$$

$$= \left( \sum_{l=1}^{n} q_l - \sum_{l=m+1}^{n} (l-m) \cdot P(X = l) \right) \cdot u_F - p_F c_p.$$ 

In what follows, we demonstrate that there exist four different types of equilibria.

**Proposition 1** An equilibrium in which the firm chooses $p_F = 0$ and all workers choose $p_{W_i} = 0$ exists if and only if

$$c_p > \max \left\{ \left( n\alpha - \sum_{l=m+1}^{n} (l-m) \cdot f(l; n, 0) \right) \cdot u_F, \alpha \cdot u_W \right\}.$$ 

Payoffs are $U_F = 0$ and $U_{W_i} = u_0$.

The intuition behind Proposition 1 is simple. If posting an ad is sufficiently costly, the benefit to posting an ad (in terms of the potential creation of a worker-firm match) is outweighed by the cost. Therefore, none of the parties is willing to post. As no worker-firm match is formed and no costs are incurred, the firm earns zero profit and each worker receives the reservation utility $u_0$. Because none of the parties posts, we call this the NP equilibrium.

We now consider the equilibria that emerge when the cost of posting an ad decreases. When this cost is sufficiently low, (at least) one party finds it optimal to post an ad. We begin with the FP equilibrium, in which only the firm posts.

**Proposition 2** An equilibrium in which the firm chooses $p_F = 1$ and each worker chooses $p_{W_i} = 0$ exists if and only if

$$\alpha (1-\alpha) \left( \sum_{l=0}^{m-1} f(l; n-1, 0) + \sum_{l=m}^{n-1} f(l; n-1, 0) \frac{m}{l+1} \right) u_W$$

$$< c_p \leq \left( n\alpha - \sum_{l=m+1}^{n} (l-m) \cdot f(l; n, 0) \right) \cdot u_F.$$ 

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Expected payoffs are

\[ U_F = \left( n\alpha - \sum_{i=m+1}^{n} (i-m) \cdot f(i; n, 0) \right) \cdot u_F - c_p \text{ and} \]

\[ U_{W_i} = \alpha \left( \sum_{l=0}^{m-1} f(l; n-1, 0) + \sum_{l=m}^{n-1} f(l; n-1, 0) \frac{m}{l+1} \right) u_W + u_0. \]

The firm and the workers could also coordinate in a different way, in which only the workers post. The following lemma and proposition characterize such a WP equilibrium.

**Lemma 1** There exists no equilibrium, in which the firm chooses \( p_F = 0 \) and exactly \( k \in \{1, ..., m-1\} \) workers choose \( p_{W_i} = 1 \).

**Proposition 3** An equilibrium in which the firm chooses \( p_F = 0 \) and exactly \( k \in \{m, ..., n-1\} \) workers choose \( p_{W_i} = 1 \) exists if and only if

(i) \( c_p > \left( n\alpha - k\alpha^2 - \sum_{l=m+1}^{n} (l-m) \cdot (f(l; n-k, k) - f(l; k, 0)) \right) \cdot u_F \),

(ii) \( c_p \leq \alpha \left( \sum_{l=0}^{m-1} f(l; k-1, 0) + \sum_{l=m}^{n-1} f(l; k-1, 0) \frac{m}{l+1} \right) u_W \) and

(iii) \( c_p > \alpha \left( \sum_{l=0}^{m-1} f(l; k, 0) + \sum_{l=m}^{n-1} f(l; k, 0) \frac{m}{l+1} \right) u_W \).

An equilibrium in which the firm chooses \( p_F = 0 \) and all workers choose \( p_{W_i} = 1 \) exists if and only if conditions (i) and (ii) are met for \( k = n \). Expected payoffs are

\[ U_F = \left( k\alpha - \sum_{l=m+1}^{n} (l-m) \cdot f(l; k, 0) \right) \cdot u_F \text{ and} \]

\[ U_{W_i} = \begin{cases} 
\alpha \left( \sum_{l=0}^{m-1} f(l; k-1, 0) + \sum_{l=m}^{n-1} f(l; k-1, 0) \frac{m}{l+1} \right) u_W + u_0 - c_p & \text{if } p_{W_i} = 1 \\
u_0 & \text{if } p_{W_i} = 0.
\end{cases} \]

Finally, there could exist a BP equilibrium in which both market sides post ads. Existence of this equilibrium requires that neither \( c_p \) nor \( \alpha \) be too high. The requirement that \( \alpha \) cannot be too high is intuitive. Consider a worker
who is considering whether to post an ad. If $\alpha$ is close to 1 the worker can be confident that he will find the ad posted by the firm, so that posting an ad is not worthwhile.

**Proposition 4** An equilibrium in which the firm chooses $p_F = 1$ and exactly $k \in \{1, ..., n - 1\}$ workers choose $p_{W_i} = 1$ exists if and only if

\[
(i) \quad c_p \leq \left( n\alpha - k\alpha^2 - \sum_{l=m+1}^{n} (l - m) \cdot (f(l; n - k, k) - f(l; k, 0)) \right) \cdot u_F,
\]

\[
(ii) \quad c_p \leq \alpha (1 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n - k, k - 1) + \sum_{l=m}^{n-1} f(l; n - k, k - 1) \frac{m - l}{l + 1} \right) u_F
\]

and

\[
(iii) \quad c_p > \alpha (1 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n - k - 1, k) + \sum_{l=m}^{n-1} f(l; n - k - 1, k) \frac{m - l}{l + 1} \right) u_F.
\]

An equilibrium in which the firm chooses $p_F = 1$ and all workers choose $p_{W_i} = 1$ exists if and only if conditions (i) and (ii) are met for $k = n$. Expected payoffs are

\[
U_F = \left( n\alpha + k\alpha (1 - \alpha) - \sum_{l=m+1}^{n} (l - m) \cdot f(l; n - k, k) \right) \cdot u_F - c_p
\]

and

\[
U_{W_i} = \begin{cases} 
\alpha (2 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n - k, k - 1) + \sum_{l=m}^{n-1} f(l; n - k, k - 1) \frac{m - l}{l + 1} \right) u_F + u_0 - c_p & \text{if } p_{W_i} = 1 \\
\alpha \left( \sum_{l=0}^{m-1} f(l; n - k - 1, k) + \sum_{l=m}^{n-1} f(l; n - k - 1, k) \frac{m - l}{l + 1} \right) u_W & \text{if } p_{W_i} = 0.
\end{cases}
\]

Although we have demonstrated that the game has multiple equilibria, for given parameter values the equilibrium and hence the predicted behavior is often unique. Before we provide a formal proof for this claim, it should be noted that workers impose negative externalities on each other. The higher the number of workers who actively post ads, the smaller is the chance for any given worker to be hired by the firm. Therefore, when many other workers post ads, a given worker has a lower incentive to post an ad himself. This result is formalized in the following lemma.

**Lemma 2** Consider two functions $a(l)$ and $b(l)$, with $l \in \{0, ..., n\}$, $a(l), b(l) \geq 0$, $\sum_{l} a(l) = \sum_{l} b(l) = 1$. Suppose that $\frac{a(l)}{b(l)}$ is strictly increasing in $l$, i.e. the
monotone likelihood ratio property applies. Let $\gamma_0, \ldots, \gamma_n$ be real numbers satisfying $\gamma_0 \geq \gamma_1 \geq \ldots \geq \gamma_n \geq 0$. Then $0 \leq \sum_0^n a(l) \gamma_l \leq \sum_0^n b(l) \gamma_l$.

Using the lemma, we obtain the following proposition.

**Proposition 5** \(a\) Whenever the NP equilibrium exists, no other type of equilibrium exists.

\(b\) Whenever the BP equilibrium exists, equilibria of type NP and FP do not exist.

\(c\) Whenever the BP equilibrium with $k < n$ exists, the only WP equilibrium that can potentially exist has $k = n$. Whenever the BP equilibrium with $k = n$ exists, the WP equilibrium does not exist.

## 5 Welfare implications

Conditional on a particular equilibrium being played, changes in the parameters affect the payoffs of workers and the firm within that equilibrium. For example, from the equilibrium payoffs displayed in Propositions 1, 2, 3, and 4, it is straightforward to see that increases in $c_p$ have a non-positive effect on the payoffs that workers and the firm receive in any equilibrium. Moreover, conditional on a particular equilibrium being played, all payoffs are continuous functions of the parameters, i.e. small changes in these parameters have a small impact on payoffs. Another interesting feature of the total welfare function is that it exhibits discontinuities that occur when a parameter change induces workers and/or the firm to behave differently, thereby causing a switch to a different equilibrium.

We use two examples to illustrate the preceding statements. First, suppose that $n = 1$ and $u_F = u_W =: u$ so that the existence conditions for equilibria NP and BP collapse to $c_p > \alpha u$ and $c_p \leq \alpha(1 - \alpha)u$, respectively. Under these assumptions the existence conditions for equilibria FP and WP are identical, namely $\alpha(1 - \alpha)u < c_p \leq \alpha u$. The expressions for total welfare in the four possible equilibria are as follows: $u_0$ for NP, $2\alpha u - c_p + u_0$ for FP or WP, and $2\alpha(2 - \alpha)u - 2c_p + u_0$ for BP. Consider a value of $c_p$ exceeding $\alpha u$, so that the existence condition for equilibrium NP is met. If $c_p$ is continuously decreased, total welfare remains constant at $u_0$ until $c_p = \alpha u$. At that point, total welfare increases discretely by the amount $2\alpha u - c_p$, when the equilibrium switches to
FP or WP. Further decreases in $c_p$ increase total welfare linearly as the side that is posting ads (either the firm or the worker) is able to do so at a lower cost, and this continues until $c_p = \alpha(1 - \alpha)u$. At that point total welfare increases discretely by the amount $2\alpha(1 - \alpha)u - c_p$. Further decreases in $c_p$ increase total welfare linearly as both sides are able to post ads at a lower cost. This example is depicted graphically in Figure 3, assuming $u = 100$, $\alpha = 0.7$, and $u_0 = 0$.

The second example, depicted graphically in Figure 4, concerns $\alpha$. Suppose $n = 1$, $c_p = 20$, $u_F = u_W = 100$, and $u_0 = 0$. Under these assumptions the existence conditions for the NP and BP equilibria collapse to $\alpha < 0.2$ and $0.2 \leq \alpha(1 - \alpha)$, respectively, whereas the FP and WP equilibria share the same existence condition, $\alpha(1 - \alpha) < 0.2 \leq \alpha$. Total welfare is 0 in equilibrium NP, $200\alpha(2 - \alpha) - 40$ in equilibrium BP, and $200\alpha - 20$ in equilibria FP and WP. Consider a value of $\alpha$ less than 0.2, so that the NP equilibrium prevails. If $\alpha$ is increased continuously, total welfare remains constant at 0 until $\alpha = 0.2$, at which point the equilibrium switches to FP or WP, and total welfare increases discretely by 20. The reason for the equilibrium switch is that $\alpha$ affects the probability of a match conditional on at least one ad being posted, and when this probability becomes high enough one side of the market becomes willing to incur posting costs, thereby creating positive externalities for the other (free riding) side of the market.\textsuperscript{21}

If $\alpha$ continues to increase, total welfare increases linearly in $\alpha$ until the equilibrium switches to BP, at which point total welfare increases discretely by $200\alpha(2 - \alpha) - 40$ and then continuously in concave fashion. The equilibrium switches in this case because $\alpha$ has finally become high enough that the free-riding side of the market receives enough private benefit from posting to justify incurring the posting cost. This private benefit derives from $\alpha(1 - \alpha)$, which is the increase in the probability that a match occurs when the free-riding side of the market decides to post an ad. When $\alpha$ is small, the free-riding side of the market cannot increase the match probability much by posting, so it is not worth incurring posting costs. Similarly, when $\alpha$ is high the incentive to free ride becomes strong again. This is because as long as one side of the market posts an ad, the likelihood that a match occurs is quite high, so the free-riding side cannot increase the match probability much by posting, and it is therefore not worth incurring posting costs. In summary, the incentive to free ride on the other side of the market is strongest for extreme values of $\alpha$.

\textsuperscript{21}In this simple example with only one worker, all externalities arising from posting are positive.
These results concerning $\alpha$ have interesting and unexpected policy implications. Focusing on the right-most discontinuity in Figure 4, small labor market interventions to increase job mobility and reduce search frictions – which intuitively would seem to enhance welfare as long as the costs of implementing the policies are modest – can in some cases lead to large reductions in welfare that arise when one side of the labor market is induced to free ride on the investments made by the other side, thereby lowering the positive externalities associated with search-related activities. Consider two alternative ways a policymaker could intervene. One is to increase $\alpha$, and the other is to decrease $c_p$. Abstracting from the costs of the alternative policies, this example suggests that the latter may be the safer choice. If the economy is in equilibrium BP, a reduction in search costs increases welfare continuously but without the risk of tipping the economy into the equilibria FP or WP which may involve a decrease in total welfare.

6 Explaining the historical evolution of job advertisements

Before applying our model to propose possible explanations for the historical evolution of advertising behavior documented in Section 2, we address some alternative explanations that were suggested to us by others. One common reaction to the pattern of evidence in Figures 1 and 2 is that it might be explained by changes in the relative bargaining power of workers and firms over time, caused either by institutions (e.g. the abolition of slavery or the introduction and growth of unions) or by market forces (i.e. shifts in supply and demand for labor). In the context of our model, changes in relative bargaining power can be interpreted as changes in the relative values of $u_F$ and $u_W$. We feel that explanations based on slavery or unions can be eliminated based on timing.\footnote{In the United States, the Emancipation Proclamation was signed in 1863, and the thirteenth amendment (abolishing slavery) was passed in 1865. But Figure 2 shows that the fraction of ads posted by employers was well under ten percent even as late as 1881. In Britain, the British Slavery Abolition Act came into force in 1834. At the time, the fraction of ads posted by employers was around ten percent. Figure 1 reveals a sharp and temporary uptick in the fraction shortly after that, but we have argued that this is likely due to the railway boom in London in the mid 1840s. In both Figures 1 and 2, all but the first few observations succeed the abolition of slavery. Similarly, union density in the United States increased until around the Second World War, peaking shortly after the war and then starting a pronounced and continuous decline. Such a trajectory could not explain Figure 2, and a}
Market forces that shift the demand and supply of labor can also be a reason for a changing balance of bargaining power between workers and firms. Perhaps when there are relatively few vacancies (job seekers) it is the job seekers (employers) who need to invest in persuasion. Our argument that the 1845 spike in Figure 1 can be attributed to the railway boom in London is consistent with labor market tightness affecting posting behavior. However, this cannot be the only (or even the main) explanation for the pattern of evidence, for at least two reasons. First, the changes in relative bargaining power resulting from shifts in labor supply and demand are cyclical. In contrast, the graphs in Figures 1 and 2 are marching steadily upward over the entire period. There has not been a dramatic, monotonic change in the supply and demand for labor over the span of more than a century, in either the United States or Britain. Second, if the explanation for Figures 1 and 2 is changes in supply and demand, the impact of the Great Depression (the most severe instance of excess labor supply in the twentieth century) should be clearly visible in posting behavior. In the United States the start of the Great Depression is typically defined to coincide with the stock market collapse in October 1929. The 1931 observation in Figure 2 occurred a full two years into the Great Depression, and there is no indication that the sharp increase in unemployment led to an increase in the fraction of ads posted by job seekers. A similar argument can be made for Britain. Furthermore, Katz and Margo (2013) cite new archival wage data suggesting that the demand for high-skilled, white collar workers grew more rapidly than supply for a period long pre-dating the Civil War and extending to the end of the nineteenth century, though the first few observations of Figure 2 do not suggest a concomitant sharp increase in the share of ads posted by employers.

Although we think it is clear that supply and demand shifts cannot explain the bulk of Figures 1 and 2, these forces seem to have played a role in 1845 in London. The question is why employers temporarily deviated from their usual behavior during the railway boom. One possibility is that the boom created a sudden and unexpected demand for a certain type of labor requiring specialized skills that are not acquired overnight (e.g. jobs as engineers or surveyors) and for which no ready substitutes are available. This situation would create a shortage of the type not often seen in the labor market. Under these circumstances,

For example, the U.S. unemployment rate was 4.3 percent in 1901 and 9.5 percent in 1911, whereas a century later it was 5.3 percent in 2001 and 8.9 percent in 2011. The first two numbers are yearly estimates from Lebergott (1957), and the latter two are from October BLS data.
many job seekers posting ads would receive multiple contacts from prospective employers, and in turn employers would frequently find that responding to a job seeker’s posting would not lead to a match. Employers for whom the returns to filling a vacancy were highest might also find it in their interests to post ads offering generous compensation (as in the examples we presented) so as to favorably distinguish themselves from competing employers. Note that the same type of reasoning would likely not apply in the case of excess labor supply. That is, a job seeker posting a willingness to accept very low wages might send a negative rather than a positive signal to prospective employers who might fear adverse selection.

Another suggestion is that the pattern of evidence in Figures 1 and 2 could be driven by technological progress that changed the nature of jobs. This might have influenced the relative importance of information about one side of the labor market versus the other, potentially changing the relative returns to posting ads. The importance of finding a high-quality match (as opposed to simply a match) might have changed due to technological progress, resulting in a change in which side of the market invested in advertising.

Our reaction to this argument is that even if a change in the returns to match quality occurred during the years covered in Figures 1 and 2, it is not obvious why that should have implications for which side of the labor market posts. Ads can be short and general or long and detailed, regardless of which side posts, and both types of ads can be found from either side of the labor market, both in the late nineteenth and late twentieth centuries. The most typical case, in either time period, is a brief ad, regardless of who posts it. Consider the following ad posted in the October 24, 1861 edition of The New York Times by a male job seeker: “AS BOOK-KEEPER. - WANTED, A SITUATION, by a thoroughly competent double-entry book-keeper of thirteen years’ practical experience; was five years with last employers. Good City reference furnished. Address WM. CHAPMAN, Powers’ Hotel.” Compare that ad to the following employer-posted ad appearing in the October 24, 2001 edition of the same newspaper: “BOOKKEEPER F/C. For sml, prestigious mdtnw office. Must have 3+ years exp MAS 90. Sal negot. FAX resume 212-752-5082.” Apart from the fact that the accounting software MAS 90 was not available in 1861, we see little difference between these ads except for which side of the labor market posted them. And the technological progress embodied in the accounting software does not seem crucial from the standpoint of which side of the labor market posts. If the software had been available in 1861, we expect that the job seeker would
have mentioned his experience with it in his ad.\textsuperscript{24} Overall, our reading of the newspapers suggests that there has been no dramatic historical shift (as measured by the nature and content of the postings) in the returns to match quality during the period covered in Figures 1 and 2, and although technology changed the nature and composition of jobs in the economy, it is unclear why this should have had a dramatic impact on which side of the labor market posts ads.

Turning to our model, the Pre-Ad era covered in Table 1 and the first three rows of Table 2 is best described by our model’s NP equilibrium. Although posts were occasionally seen during this period on either side of the market, they were quite rare. What followed was an era of regularly posted ads, dominated by worker-posted ads, that lasted roughly throughout the nineteenth century. Recall from Table 3 that the average fraction of ads posted by New York City employers was less than 5 percent in the years 1861, 1871, and 1881. Keeping in mind that the number of workers that are looking for a job exceeds the number of firms that hire workers, our BP equilibrium can be thought of as an approximation to this situation. As noted earlier, another possibility is that equilibria FP and WP occur simultaneously, implying that the structure of the game resembles that of “battle of the sexes”. The observed behavior could then be explained in two ways: either some people failed to coordinate on the correct equilibrium or some occupations and industries played equilibrium FP whereas others played WP. We now turn to a potential explanation for the shift from the Pre-Ad era characterized by the NP equilibrium to the Early era characterized by the BP equilibrium (or the joint occurrence of equilibria FP and WP). Our impression is that the timing of this transition suggests that it arose from increases in literacy rates (driven by the Industrial Revolution and the growth of public schools).

As Tables 1 and 2 reveal, the NP equilibrium clearly prevailed around 1760 at the start of the Industrial Revolution, whereas by the end of the Industrial Revolution the new era of regularly posted ads was emerging. The technological innovations of the Industrial Revolution brought new manufacturing processes that lowered the production costs of paper, books, and other printed materials, making them more affordable for all social classes. These changes facilitated

\textsuperscript{24}Our book keepers example focuses on a job that existed in both time periods. It is true that technological progress changed the composition of jobs in the economy as well as the nature of particular jobs. For example, there are no ads for coachmen in the late twentieth century, whereas there are many in the 1860s. But there are modern counterparts to most jobs (e.g. the coachmen of the nineteenth century are the bus, cab, and limousine drivers of the twentieth century), so similar arguments can be made.
improvements in literacy rates. In the context of our model, a situation in which most of the economic agents are illiterate can be thought of as one in which \( \beta \) is extremely low. In the extreme case, \( \beta \) is equal to zero which means that all job seekers are illiterate. Obviously, posting an ad is neither optimal for the firm nor for the workers in this situation, so that the NP equilibrium prevails. When literacy expanded (because of the Industrial Revolution), the costs of posting ads dropped substantially for the workers who became literate. As a consequence, it is conceivable that the WP equilibrium emerged, with workers demonstrating their newly acquired skills by posting ads and firms looking for these worker-posted ads.

Further promulgating literacy, in New York City the education system became public in every respect when the schools of the Public School Society were turned over to the city’s first Board of Education (established in 1842), propelling the system in both growth and effectiveness for the remainder of the century (Palmer 1905). By 1904 the city’s system had 546 school buildings, more than 13,000 teachers, a growing registration of 622,000 students, and national recognition for quality (Palmer 1905). In London, the Newcastle Report of 1861 urged the provision of “sound and cheap” elementary schools for working class children between the ages of 5 and 13, and in 1870 Parliament passed the Elementary Education Act (The Forster Act) to implement those recommendations (Gillard 2009).

A similar argument to the preceding can explain the transition from the Modern era to the Internet era that occurred in the late twentieth and early twenty-first centuries. The advent of the internet led to a significant decrease in the costs of posting and reading ads. This led to a transition from the FP equilibrium in which employers posted ads to the BP equilibrium in which

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25 As noted in West (1978), “It is generally agreed by all participants that people were more literate at the end of the Industrial Revolution period, 1760-1840, than they were at the beginning.” See also Figure 1 of that study, which documents a sharp decrease in the annual percentage of males and females unable to sign at marriage, in England and Wales from 1839 to 1912, and Figure 2, which documents a sharp decrease in the annual percentages of illiterate male and female school leavers (as determined by their inability to sign the marriage register 15 years later) from 1820 to 1900.

26 In 1904 New York City’s schools won multiple gold medals at the Louisiana Purchase Exposition in Missouri, and in the same year Harvard’s president (Charles William Eliot) stated that “New York City has produced a system of public instruction which the whole country may well copy.” (Palmer 1905)

27 Lower costs have also facilitated greater detail in the content of employment-related postings, company and personal websites, and Facebook pages. Brenčič and Norris (2009) find that the average length of an online job description is about 2553 characters long (about one page), which significantly exceeds the length of the typical job ad that was printed historically in the newspaper.
both firms and job seekers post (online) ads. Figure 3 illustrates, for a particular configuration of parameters, how the equilibria switch as the posting cost decreases, as in our explanation for the Pre-Ad-to-Early transition and for the Modern-to-Internet transition. In the following subsections we propose three complementary explanations for the transition from the Early era to the Modern era.

6.1 Growth in firm size and the labor force

As Figure 2 in Poschke (2011) shows for the US, firms have grown in size over time, and the biggest growth seems to have occurred between 1940 and 1980. At the same time, the labor force has also grown in size. These simple observations have the potential to explain the historical change in advertising behavior. In our model, an increase in firm size can be captured by an increase in \( m \), whereas an increase in the size of the labor force is captured by an increase in \( N \) which causes an increase in \( n \). First consider the Early era. Suppose that

\[ (*) \quad c_p \leq \left( n \alpha (1 - \alpha) - \sum_{l=m+1}^{n} (l - m) \cdot (f(l; 0, n) - f(l; n, 0)) \right) \cdot u_F \] and

\[ (**) \quad c_p \leq \alpha (1 - \alpha) \left( \sum_{l=0}^{m-1} f(l; 0, n - 1) + \sum_{l=m}^{n-1} f(l; 0, n - 1) \cdot \frac{m}{l+1} \right) u_W. \]

Then the BP equilibrium with \( k = n \) is the only equilibrium that exists, so that we observe both firms and workers posting ads. Next consider the Modern era and assume that both \( m \) and \( n \) have increased. The existence condition of the firm in the FP equilibrium can be stated as

\[ c_p \leq \left( \sum_{l=1}^{m} l \cdot f(l; n, 0) + m \sum_{l=m+1}^{n} f(l; n, 0) \right) \cdot u_F. \]

It is straightforward to show that the term on the right-hand-side of the condition is increasing in both \( m \) and \( n \), indicating that the changes in \( m \) and \( n \) have increased the firm’s incentive to post ads.\(^{28}\) Similarly, one can show that the increase in \( m \) increases a worker \( i \)’s incentive to post an ad (because the ad is

\[ g(m+1, n) - g(m, n) = \binom{n}{m+1} \alpha^{m+1} (1 - \alpha)^{n-m-1} + \sum_{l=m+2}^{n} \binom{n}{l} \alpha^l (1 - \alpha)^{n-l} > 0 \]

\(^{28}\)To see this, define \( g(m, n) := \sum_{l=1}^{m} l \cdot f(l; n, 0) \). It can be shown that
more likely to lead to a successful match), whereas the incentive to post an ad is decreasing in \( n \) (since competition among the workers discourages them due to a negative externality). When the latter effect dominates, it is conceivable that in consequence of the changes in \( m \) and \( n \), the BP equilibrium no longer exists. Instead, the FP equilibrium may become feasible so that we only observe firms posting ads, as was true in London and New York in the early 1990s, as seen in Figures 1 and 2.

### 6.2 Job mobility and search frictions

Search frictions and impediments to worker mobility have decreased over time, due to the increasing dissemination of information and to a reduction in transportation costs. In the context of our model, a reduction in search frictions implies an increase in \( \alpha \). Such a change could explain the historical evolution of advertising behavior. First, consider the Early era, and suppose that \((*)\), \((**\)) and \( \alpha > 0.5 \) hold. In this case the BP equilibrium with \( k = n \) is the only equilibrium that exists, so that we observe both firms and workers posting ads. Next consider the Modern era. The increase in \( \alpha \) over time implies that \( c_p \leq \alpha (1 - \alpha) \left( \sum_{l=0}^{m-1} f (l; n-1, 0) + \sum_{l=m}^{n-1} f (l; n-1, 0) \frac{m}{l+1} \right) u_W \) is violated.\(^29\) Accordingly, the BP equilibrium no longer exists (for any value of \( k \)).

As described in Section 5, the intuition for a worker who expects the firm to post an ad is as follows: By posting an ad, the worker increases the probability of making contact from \( \alpha \) to \( 2\alpha - \alpha^2 \) but also incurs the posting cost. If \( \alpha \) is relatively high, the probability difference \( 2\alpha - \alpha^2 - \alpha = \alpha (1 - \alpha) \) is low, so that the worker is not willing to incur the posting cost. By the same token, it is likely that the FP equilibrium exists in the new situation. In this equilibrium, only the firm invests, and when \( \alpha \) is high the incentive for the firm to invest is high. This can explain why we observe only firms posting ads in the late twentieth century.

\[ g(m, n + 1) - g(m, n) = \sum_{l=0}^{m-1} \binom{n}{l} \alpha^{l+1} (1 - \alpha)^{n-l} > 0. \]

\(^29\) Define \( \Phi(\alpha) := \left( \sum_{l=0}^{m-1} f (l; n-1, 0) + \sum_{l=m}^{n-1} f (l; n-1, 0) \frac{m}{l+1} \right) \) and notice that \( \frac{\partial(1 - \alpha) \Phi(\alpha)}{\partial(\alpha (1 - \alpha) \Phi(\alpha))} = (1 - 2\alpha) \Phi(\alpha) + \alpha (1 - \alpha) \Phi'(\alpha) \). The first term is negative because of \( \alpha > 0.5 \) and the second term is negative because of Lemma 2.
6.3 Incremental gain from being hired

It is likely that the difference in utility from being hired by a firm versus being unemployed has decreased over time. This is because around the turn of the twentieth century the absence of social security systems meant that unemployment imposed particularly high costs on workers. As the twentieth century progressed and social security systems developed (e.g. the New Deal policies of the US in the 1930s), the costs of being unemployed diminished. In the context of the model, this implies that $u_0$ became higher and, as a consequence, $u_W$ became lower between the Early and Modern eras. This can explain the historical shift in the pattern of job advertisements. First, consider the Early era, and suppose again that $(*)$ and $(**)$ are met, so that the BP equilibrium with $k = n$ is played. Next consider the Modern era. Compared with the Early era, $u_W$ has decreased over time so that the second of the above conditions is now violated and even $c_p \leq \alpha u_W$ does not hold. Accordingly, equilibria of types BP and WP do not exist. Intuitively, because of the development of social security systems and the resulting decrease in $u_W$, workers are no longer willing to incur the cost of posting an ad. The FP equilibrium, however, exists and is played. Therefore, we only observe firms posting ads in the late twentieth century.

7 Concluding Remarks

To understand the four eras of advertising history that we have documented and the transitions across them, we developed a theoretical framework emphasizing strategic interactions in the search-related investments of job seekers and employers. A direct consequence of accounting for strategic behavior is discontinuity and non-monotonicity in the social welfare function, which has a number of potentially important policy implications, some of which we have highlighted. Our model shows that small policy changes can have large effects on welfare and that the predicted effect of a policy change depends on which side of the labor market invests in search-related activities. Seemingly innocuous policies like those aimed at increasing job mobility and reducing search frictions can have the unintended consequence of inducing one side of the market to free ride on the investments of the other, thereby reducing positive externalities and welfare. Alternative policy interventions aimed at reducing search-related costs are not subject to those risks.

The analysis illustrates how history can deepen our understanding of the
functioning of labor markets. Dramatic changes in the search-related activities of employers and job seekers have occurred over time, permitting illuminating inquiry into the reasons for those changes. But these patterns of evidence emerged only when the historical clock was turned back a considerable time, unveiling secrets buried in a stack of old newspapers.
Appendix

Proof of Proposition 1. Assume that the firm chooses \( p_F = 0 \) and all workers choose \( p_{W_i} = 0 \). We have \( q_i = 0 \) for all \( i \), so that \( U_F = 0 \) and \( U_{W_i} = u_0 \). If the firm deviates to \( p_F = 1 \), each of the \( q_i \) equals \( \alpha \). It follows that \( P(X = l) = f(l; n, 0) \), and the firm’s expected payoff becomes

\[
U_F = \left( n\alpha - \sum_{l=m+1}^{n} (l - m) \cdot f(l; n, 0) \right) \cdot u_F - c_p.
\]

Such a deviation is unprofitable if and only if

\[
c_p > \left( n\alpha - \sum_{l=m+1}^{n} (l - m) \cdot f(l; n, 0) \right) \cdot u_F.
\]

Suppose now that worker \( i \) deviates to \( p_{W_i} = 1 \), in which case we have \( q_i = \alpha \) and \( q_j = 0 \) for all \( j \neq i \). Therefore, the worker’s expected payoff becomes \( U_{W_i} = \alpha u_W + u_0 - c_p \). Such a deviation is not profitable if and only if \( c_p > \alpha \cdot u_W \).

Proof of Proposition 2. From the proof of Proposition 1, it follows immediately that the firm prefers \( p_F = 1 \) to \( p_F = 0 \) if and only if

\[
c_p \leq \left( n\alpha - \sum_{l=m+1}^{n} (l - m) \cdot f(l; n, 0) \right) \cdot u_F.
\]

Consider worker \( i \). In equilibrium we have \( q_j = \alpha \) for all \( j \). Hence, the worker’s expected equilibrium payoff is

\[
U_{W_i} = \alpha \left( \sum_{l=0}^{m-1} f(l; n-1, 0) + \sum_{l=m}^{n-1} f(l; n-1, 0) \frac{m}{l+1} \right) u_W + u_0.
\]

If worker \( i \) decided to deviate to \( p_{W_i} = 1 \), \( q_i \) would increase to \( \alpha \cdot (2 - \alpha) \), whereas we still had \( q_j = \alpha \) for all \( j \neq i \). Worker \( i \)’s payoff in case of a deviation thus becomes

\[
U_{W_i} = \alpha \left( 2 - \alpha \right) \left( \sum_{l=0}^{m-1} f(l; n-1, 0) + \sum_{l=m}^{n-1} f(l; n-1, 0) \frac{m}{l+1} \right) u_W + u_0 - c_p.
\]
Therefore, a deviation is not profitable if and only if

\[ \alpha (1 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n-1, 0) + \sum_{l=m}^{n-1} f(l; n-1, 0) \frac{m}{l+1} \right) u_W < c_p. \]

\[ \text{Proof of Lemma 1.} \quad \text{If} \ k \in \{1, \ldots, m-1\} \ \text{workers choose} \ p_{W_i} = 1 \ \text{and, hence,}\]
\[ \text{prefer to choose} \ p_{W_i} = 1 \ \text{instead of} \ p_{W_i} = 0, \ \text{at least one of the remaining}\]
\[ \text{workers would like to deviate from} \ p_{W_i} = 0 \ \text{to} \ p_{W_i} = 1. \]

\[ \text{Proof of Proposition 3.} \quad \text{In equilibrium we have} \ q_i = \begin{cases} \alpha & \text{if} \ p_{W_i} = 1 \\ 0 & \text{if} \ p_{W_i} = 0 \end{cases}. \]

Thus, the firm’s expected equilibrium payoff is

\[ U_F = \left( k\alpha - \sum_{l=m+1}^n (l - m) \cdot f(l; k; 0) \right) \cdot u_F. \]

If the firm were to deviate to \( p_F = 1 \), \( q_i \) would become

\[ q_i = \begin{cases} \alpha (2 - \alpha) & \text{if} \ p_{W_i} = 1 \\ \alpha & \text{if} \ p_{W_i} = 0 \end{cases}. \]

The firm’s expected payoff would change to

\[ U_F = \left( k\alpha (2 - \alpha) + (n - k) \alpha - \sum_{l=m+1}^n (l - m) \cdot f(l; n-k, k) \right) \cdot u_F - c_p. \]

The firm has no incentive to deviate if and only if

\[ c_p > \left( n\alpha - k\alpha^2 - \sum_{l=m+1}^n (l - m) \cdot (f(l; n-k, k) - f(l; k, 0)) \right) \cdot u_F. \]

Consider now a worker who has chosen \( p_{W_i} = 1 \). The worker’s expected equilibrium payoff is

\[ U_{W_i} = \alpha \left( \sum_{l=0}^{m-1} f(l; k-1, 0) + \sum_{l=m}^{n-1} f(l; k-1, 0) \cdot \frac{m}{l+1} \right) u_W + u_0 - c_p. \]

In case of a deviation to \( p_{W_i} = 0 \) the worker would receive his reservation utility \( u_0 \). Hence, a deviation is not profitable if and only if

\[ \alpha \left( \sum_{l=0}^{m-1} f(l; k-1, 0) + \sum_{l=m}^{n-1} f(l; k-1, 0) \cdot \frac{m}{l+1} \right) u_W \geq c_p. \]
Finally, consider a worker who has chosen $p_{Wi} = 0$ and thus receives $u_0$ in equilibrium. In case of a deviation to $p_{Wi} = 1$ the worker’s expected payoff would become

$$U_{Wi} = \alpha \left( \sum_{l=0}^{m-1} f(l; k, 0) + \sum_{l=m}^{n-1} f(l; k, 0) \frac{m}{l+1} \right) u_W + u_0 - c_p.$$ 

Thus, a deviation is not profitable if and only if

$$\alpha \left( \sum_{l=0}^{m-1} f(l; k, 0) + \sum_{l=m}^{n-1} f(l; k, 0) \frac{m}{l+1} \right) u_W < c_p.$$ 

\[\blacksquare\]

**Proof of Proposition 4.** In equilibrium we have $q_i = \begin{cases} \alpha (2 - \alpha) & \text{if } p_{Wi} = 1 \\ \alpha & \text{if } p_{Wi} = 0 \end{cases}$. Thus, the firm’s expected equilibrium payoff is

$$U_F = \left( k\alpha (2 - \alpha) + (n - k)\alpha - \sum_{l=m+1}^{n} (l - m) \cdot f(l; n - k, k) \right) \cdot u_F - c_p$$

$$= \left( n\alpha + k\alpha (1 - \alpha) - \sum_{l=m+1}^{n} (l - m) \cdot f(l; n - k, k) \right) \cdot u_F - c_p.$$ 

If the firm were to deviate to $p_F = 0$, $q_i$ would become $q_i = \begin{cases} \alpha & \text{if } p_{Wi} = 1 \\ 0 & \text{if } p_{Wi} = 0 \end{cases}$, and the firm’s expected payoff would change to

$$U_F = \left( k\alpha - \sum_{l=m+1}^{n} (l - m) \cdot f(l; k, 0) \right) \cdot u_F.$$ 

The firm has no incentive to deviate if and only if

$$c_p \leq \left( n\alpha - k\alpha^2 - \sum_{l=m+1}^{n} (l - m) \cdot (f(l; n - k, k) - f(l; k, 0)) \right) \cdot u_F.$$ 

Consider now a worker who has chosen $p_{Wi} = 1$. The worker’s expected equilibrium payoff is

$$U_{Wi} = \alpha (2 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n - k, k - 1) + \sum_{l=m}^{n-1} f(l; n - k, k - 1) \frac{m}{l+1} \right) u_W + u_0 - c_p.$$
In case of a deviation to $p_{Wi} = 0$ the worker’s expected payoff would change to

$$U_{Wi} = \alpha \left( \sum_{l=0}^{m-1} f(l; n - k, k - 1) + \sum_{l=m}^{n-1} f(l; n - k, k - 1) \frac{m-1}{l+1} \right) u_W + u_0.$$ 

Hence, a deviation is not profitable if and only if

$$\alpha (1 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n - k, k - 1) + \sum_{l=m}^{n-1} f(l; n - k, k - 1) \frac{m}{l+1} \right) u_W \geq c_p.$$ 

Finally, consider a worker who has chosen $p_{Wi} = 0$ and thus receives equilibrium payoff equal to

$$U_{Wi} = \alpha \left( \sum_{l=0}^{m-1} f(l; n - k - 1, k) + \sum_{l=m}^{n-1} f(l; n - k - 1, k) \frac{m}{l+1} \right) u_W + u_0.$$ 

In case of a deviation to $p_{Wi} = 1$ the worker’s expected payoff would become

$$U_{Wi} = \alpha (2 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n - k - 1, k) + \sum_{l=m}^{n-1} f(l; n - k - 1, k) \frac{m}{l+1} \right) u_W + u_0 - c_p.$$ 

Thus, a deviation is not profitable if and only if

$$\alpha (1 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n - k - 1, k) + \sum_{l=m}^{n-1} f(l; n - k - 1, k) \frac{m}{l+1} \right) u_W < c_p.$$ 

$\blacksquare$

**Proof of Lemma 2.** Since all variables are nonnegative, it is obvious that $0 \leq \sum_l a(l) \gamma_l$. It remains to be shown that

$$\sum_l (b(l) - a(l)) \gamma_l \geq 0.$$ 

Define $\Delta(l) := b(l) - a(l)$. Since $\sum_l a(l) = \sum_l b(l)$ and $\frac{n(l)}{u(l)}$ is strictly increasing in $l$, there must be some $\hat{l} \in \{0, ..., n\}$ such that $\Delta(l) \geq 0$ for $l \leq \hat{l}$. We can
then restate \( \sum_l \Delta(l) \gamma_l \) as

\[
\sum_l \Delta(l) \gamma_l + \sum_{l < \hat{l}} \Delta(l) (\gamma_l - \gamma_{\hat{l}}) + \sum_{l > \hat{l}} \Delta(l) (\gamma_{\hat{l}} - \gamma_l)
\]

\[
= \sum_{l < \hat{l}} \Delta(l) (\gamma_l - \gamma_{\hat{l}}) + \sum_{l > \hat{l}} \Delta(l) (\gamma_{\hat{l}} - \gamma_l).
\]

For \( l < \hat{l} \), we have \( \Delta(l) > 0 \) and \( (\gamma_l - \gamma_{\hat{l}}) \geq 0 \). For \( l > \hat{l} \), we have \( \Delta(l) < 0 \) and \( (\gamma_{\hat{l}} - \gamma_l) \leq 0 \). Hence, \( \sum_{l < \hat{l}} \Delta(l) (\gamma_l - \gamma_{\hat{l}}) + \sum_{l > \hat{l}} \Delta(l) (\gamma_{\hat{l}} - \gamma_l) \) is always nonnegative.

\[\text{Proof of Proposition 5.} \]

(a) Suppose that the NP equilibrium exists, which implies

\[(i) \quad c_p > \left( n\alpha - \sum_{l=m+1}^{n} (l-m) \cdot f(l; n, 0) \right) \cdot u_F \quad \text{and} \quad (ii) \quad c_p > \alpha \cdot u_W.\]

Because of (i) the FP equilibrium does not exist. Notice that \( \sum_{l=0}^{m-1} f(l; k-1, 0) + \sum_{l=m}^{n-1} f(l; k-1, 0) \cdot \frac{m}{l+1} \leq 1 \), regardless of the exact realization of \( k \). Hence, we observe

\[c_p > \alpha \left( \sum_{l=0}^{m-1} f(l; k-1, 0) + \sum_{l=m}^{n-1} f(l; k-1, 0) \cdot \frac{m}{l+1} \right) \cdot u_W,\]

and the WP equilibrium does not exist either. Similarly, we have

\[\left( \sum_{l=0}^{m-1} f(l; n-k, k-1) + \sum_{l=m}^{n-1} f(l; n-k, k-1) \cdot \frac{m}{l+1} \right) \leq 1\]

for all \( k \in \{1, ..., n\} \), so that

\[c_p > \alpha (1 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n-k, k-1) + \sum_{l=m}^{n-1} f(l; n-k, k-1) \cdot \frac{m}{l+1} \right) \cdot u_W,\]

violating the existence conditions of the BP equilibrium.

(b) Suppose that the BP equilibrium exists. From the preceding proposition we can conclude that the NP equilibrium does not exist. Existence of the BP
equilibrium implies
\[ c_p \leq \alpha (1 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n-k, k-1) + \sum_{l=m}^{n-1} f(l; n-k, k-1) \frac{m}{l+1} \right) u_W. \]

Because of Lemma 2 we know that
\[
\sum_{l=0}^{m-1} f(l; n-1, 0) + \sum_{l=m}^{n-1} f(l; n-1, 0) \frac{m}{l+1} \\
\geq \sum_{l=0}^{m-1} f(l; n-k, k-1) + \sum_{l=m}^{n-1} f(l; n-k, k-1) \frac{m}{l+1}.
\]

Hence, it follows that
\[ c_p \leq \alpha (1 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n-1, 0) + \sum_{l=m}^{n-1} f(l; n-1, 0) \frac{m}{l+1} \right) u_W, \]

implying that the FP equilibrium does not exist.

(c) Existence of the BP equilibrium implies

(i) \[ c_p \leq \left( n\alpha - k\alpha^2 - \sum_{l=m+1}^{n} (l - m) \cdot (f(l; n-k, k) - f(l; k, 0)) \right) \cdot u_F \]
and
(ii) \[ c_p \leq \alpha (1 - \alpha) \left( \sum_{l=0}^{m-1} f(l; n-k, k-1) + \sum_{l=m}^{n-1} f(l; n-k, k-1) \frac{m}{l+1} \right) u_W. \]

Because of Lemma 2 we observe that for any \( k_W \in \{1, \ldots, n-1\} \) and \( k_B \in \{1, \ldots, n\} \)
\[
\sum_{l=0}^{m-1} f(l; k_W, 0) + \sum_{l=m}^{n-1} f(l; k_W, 0) \frac{m}{l+1} \\
\geq \sum_{l=0}^{m-1} f(l; n-k_B, k_B - 1) + \sum_{l=m}^{n-1} f(l; n-k_B, k_B - 1) \frac{m}{l+1}.
\]

Accordingly, condition (ii) implies
\[ c_p < \alpha \left( \sum_{l=0}^{m-1} f(l; k_W, 0) + \sum_{l=m}^{n-1} f(l; k_W, 0) \frac{m}{l+1} \right) u_W, \]
so that any WP equilibrium with \( k_W < n \) does not exist.
To demonstrate that a WP equilibrium with $k_W = n$ can potentially exist, consider an example with $m = 1$ and $n = 2$. Consider the BP equilibrium with $k_B = 1$ and the WP equilibrium with $k_W = 2$. The former equilibrium exists if and only if

$$c_p \leq (2\alpha - \alpha^2) \cdot u_F,$$

$$c_p \leq \alpha (1 - \alpha) \left(1 - \frac{\alpha}{2}\right) u_W \text{ and }$$

$$c_p > \alpha (1 - \alpha) \left(1 - \frac{\alpha (2 - \alpha)}{2}\right) u_W.$$

The latter equilibrium exists if and only if

$$c_p > \left(2\alpha - \alpha^2 - \alpha^2 (2 - \alpha)^2\right) \cdot u_F \text{ and }$$

$$c_p \leq \alpha \left(1 - \frac{\alpha}{2}\right) u_W.$$

Since

$$\left(2\alpha - \alpha^2 - \alpha^2 (2 - \alpha)^2\right) < (2\alpha - \alpha^2) \text{ and }$$

$$\alpha (1 - \alpha) \left(1 - \frac{\alpha (2 - \alpha)}{2}\right) < \alpha (1 - \alpha) \left(1 - \frac{\alpha}{2}\right) < \alpha \left(1 - \frac{\alpha}{2}\right),$$

there always exist parameter values for $u_F$, $u_W$ and $c_p$ such that all the five conditions are met.

Finally, suppose that $k_B = n$ so that (i) becomes

$$c_p \leq \left(n\alpha - n\alpha^2 - \sum_{l=m+1}^{n} (l - m) \cdot (f(l; 0, n) - f(l; n, 0))\right) \cdot u_F.$$

Obviously, this contradicts the existence conditions of the WP equilibrium with $k_W = n$ which require

$$c_p > \left(n\alpha - n\alpha^2 - \sum_{l=m+1}^{n} (l - m) \cdot (f(l; 0, n) - f(l; n, 0))\right) \cdot u_F.$$
References


<table>
<thead>
<tr>
<th>Year</th>
<th>Issues</th>
<th>Newspapers</th>
<th>Location</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1609</td>
<td>various</td>
<td>Relation aller Fürnemmen und gedenckwürdigen Historien</td>
<td>Strasbourg, Holy Roman Empire</td>
<td>World's first newspaper, starting in 1605 and published in Germany.</td>
</tr>
<tr>
<td>1665 - 1666</td>
<td>various</td>
<td>Oxford Gazette</td>
<td>England</td>
<td>Published in Germany, starting in 1665 and still in circulation.</td>
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<tr>
<td>1703</td>
<td>various</td>
<td>Wiener Zeitung</td>
<td>Austria</td>
<td>From issue 4 in 1666.</td>
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<tr>
<td>1708 - 1712</td>
<td>various</td>
<td>Dublin Gazette</td>
<td>Ireland</td>
<td>Thursday and Friday</td>
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<tr>
<td>1721 - January 8-15</td>
<td>various</td>
<td>New England Courant</td>
<td>Massachusetts Bay</td>
<td>Notes</td>
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<td>1722</td>
<td>September 12</td>
<td>Weekly Jamaica Courant</td>
<td>Jamaica</td>
<td>Notes</td>
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<td>1718</td>
<td>July 30</td>
<td>New England Courant</td>
<td>Massachusetts Bay</td>
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<tr>
<td>1712</td>
<td>July 30</td>
<td>London Gazette</td>
<td>England</td>
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Table 1: Employment-Related Advertising in Various Seventeenth and Eighteenth Century Newspapers.
<table>
<thead>
<tr>
<th>Location</th>
<th>Advertised by</th>
<th>Ad text</th>
<th>Quantity</th>
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<tbody>
<tr>
<td>South Carolina</td>
<td>A job seeker</td>
<td>'Two Negro Women' to be advertised by 'Two Job Seekers' for 'Two' labor</td>
<td>1</td>
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<tr>
<td>Pennsylvania</td>
<td>N/A</td>
<td>In one instance, same ad text is offered for a job seeker; a servant's services in an ad posted to buy and sell labor</td>
<td>2</td>
</tr>
<tr>
<td>South Carolina</td>
<td>N/A</td>
<td>In one instance, same ad text is offered for a job seeker; a servant's services in an ad posted to buy and sell labor</td>
<td>2</td>
</tr>
<tr>
<td>Maryland</td>
<td>N/A</td>
<td>Ad posted by 'job seeker'. A servant's time is offered for sale.</td>
<td>2</td>
</tr>
<tr>
<td>Virgin Islands</td>
<td>N/A</td>
<td>One of the posts is the advertised sale of a slave.</td>
<td>1</td>
</tr>
<tr>
<td>Delaware</td>
<td>N/A</td>
<td>One of the posts is the advertised sale of a slave.</td>
<td>1</td>
</tr>
<tr>
<td>Maryland</td>
<td>N/A</td>
<td>One of the posts is the advertised sale of a slave.</td>
<td>1</td>
</tr>
<tr>
<td>Virginia</td>
<td>N/A</td>
<td>One of the posts is the advertised sale of a slave.</td>
<td>1</td>
</tr>
<tr>
<td>Pennsylvania</td>
<td>N/A</td>
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<td>One of the posts is the advertised sale of a slave.</td>
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<td>--------</td>
<td>-------------------------------</td>
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<td>none</td>
<td>Hired Out</td>
<td>New York</td>
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<td>November 23</td>
<td>none</td>
<td></td>
<td>Ireland</td>
</tr>
<tr>
<td>January 25</td>
<td>0</td>
<td>Barbados Mercury</td>
<td>Barbados</td>
</tr>
<tr>
<td>March 1, 8, 15</td>
<td>4</td>
<td>Barbados Mercury</td>
<td>Barbados</td>
</tr>
<tr>
<td>March 22, 29</td>
<td>4</td>
<td>Barbados Mercury</td>
<td>Barbados</td>
</tr>
<tr>
<td>January 25</td>
<td>1</td>
<td>Barbados Mercury</td>
<td>Barbados</td>
</tr>
<tr>
<td>October 24</td>
<td>0</td>
<td>Barbados Mercury</td>
<td>Barbados</td>
</tr>
<tr>
<td>October 24</td>
<td>0</td>
<td>Barbados Mercury</td>
<td>Barbados</td>
</tr>
<tr>
<td>October 27</td>
<td>0</td>
<td>Barbados Mercury</td>
<td>Barbados</td>
</tr>
<tr>
<td>November 13</td>
<td>1</td>
<td>Barbados Mercury</td>
<td>Barbados</td>
</tr>
</tbody>
</table>

Contractors sought to cover the top of the "Magazine at St. Ann's" with copper.

Precursor to The Times, which still circulates.
<table>
<thead>
<tr>
<th>Year</th>
<th>Date</th>
<th>Adverts from Employers</th>
<th>Adverts from Job Seekers</th>
<th>% Ads from Employers</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1785</td>
<td>Mon, Oct 24</td>
<td>none</td>
<td>none</td>
<td>N/A</td>
<td>founded on January 1, 1785 as The Daily Universal Register</td>
</tr>
<tr>
<td>1795</td>
<td>Sat, Oct 24</td>
<td>none</td>
<td>none</td>
<td>N/A</td>
<td>changed name to The Times on January 1, 1788</td>
</tr>
<tr>
<td>1805</td>
<td>Thurs, Oct 24</td>
<td>2</td>
<td>1</td>
<td>66.7</td>
<td>front page had 3 ads, very first entry of the newspaper in column 1 of</td>
</tr>
<tr>
<td>1815</td>
<td>Tues, Oct 24</td>
<td>1</td>
<td>22</td>
<td>4.3</td>
<td>23 ads under &quot;Advertisements, etc. Vacant&quot;, ads under &quot;Advertisements, etc. Wanted&quot;, ads under &quot;Advertisements, etc. Places&quot;</td>
</tr>
<tr>
<td>1825</td>
<td>Mon, Oct 24</td>
<td>13</td>
<td>47</td>
<td>21.7</td>
<td>many ads from both sides randomly mixed together with other ads</td>
</tr>
<tr>
<td>1835</td>
<td>Sat, Oct 24</td>
<td>4</td>
<td>29</td>
<td>12.2</td>
<td>38 ads posted by either side are sprinkled throughout the first page, and</td>
</tr>
<tr>
<td>1845</td>
<td>Fri, Oct 24</td>
<td>81</td>
<td>108</td>
<td>42.9</td>
<td>many more ads posted by job seekers</td>
</tr>
<tr>
<td>1855</td>
<td>Wed, Oct 24</td>
<td>149</td>
<td>704</td>
<td>17.5</td>
<td>many ads from both sides randomly mixed together with other ads</td>
</tr>
<tr>
<td>1865</td>
<td>Tues, Oct 24</td>
<td>145</td>
<td>436</td>
<td>25.0</td>
<td>many ads from both sides randomly mixed together with other ads</td>
</tr>
<tr>
<td>1875</td>
<td>Sat, Oct 23</td>
<td>90</td>
<td>248</td>
<td>26.6</td>
<td>many more ads posted by job seekers</td>
</tr>
<tr>
<td>1885</td>
<td>Sat, Oct 24</td>
<td>39</td>
<td>126</td>
<td>23.6</td>
<td>many more ads posted by job seekers</td>
</tr>
<tr>
<td>1895</td>
<td>Thurs, Oct 24</td>
<td>26</td>
<td>64</td>
<td>28.9</td>
<td>26 ads under &quot;Advertisements, etc. Vacant&quot;, ads under &quot;Advertisements, etc. Places&quot;</td>
</tr>
<tr>
<td>1905</td>
<td>Tues, Oct 24</td>
<td>24</td>
<td>81</td>
<td>22.9</td>
<td>50 &quot;Wanted Places&quot; ads posted by job seekers</td>
</tr>
<tr>
<td>1915</td>
<td>Mon, Oct 25</td>
<td>69</td>
<td>56</td>
<td>55.2</td>
<td>24 &quot;Wanted Places&quot; ads posted by job seekers</td>
</tr>
<tr>
<td>1925</td>
<td>Sat, Oct 24</td>
<td>129</td>
<td>128</td>
<td>50.2</td>
<td>132 ads under &quot;Advertisements, etc. Vacant&quot;, ads under &quot;Advertisements, etc. Places&quot;</td>
</tr>
<tr>
<td>1935</td>
<td>Thurs, Oct 24</td>
<td>132</td>
<td>138</td>
<td>48.9</td>
<td>44 ads under &quot;Advertisements, etc. Vacant&quot;, ads under &quot;Advertisements, etc. Places&quot;</td>
</tr>
<tr>
<td>1945</td>
<td>Wed, Oct 24</td>
<td>44</td>
<td>15</td>
<td>74.6</td>
<td>late London edition</td>
</tr>
<tr>
<td>1955</td>
<td>Wed, Oct 24</td>
<td>89</td>
<td>27</td>
<td>22.9</td>
<td>43 ads under &quot;Advertisements, etc. Vacant&quot;, ads under &quot;Advertisements, etc. Places&quot;</td>
</tr>
</tbody>
</table>

Table 2: Employment-Related Advertising: A Tour Through The (London) Times
<table>
<thead>
<tr>
<th>Year</th>
<th>Date</th>
<th>Pages</th>
<th>Number</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1955</td>
<td>Sun, Oct 24</td>
<td>130</td>
<td>78</td>
<td>62.5 Royal edition</td>
</tr>
<tr>
<td>1965</td>
<td>Mon, Oct 24</td>
<td>113</td>
<td>41</td>
<td>73.4 Late London edition</td>
</tr>
<tr>
<td>1975</td>
<td>Fri, Oct 24</td>
<td>126</td>
<td>11</td>
<td>92.0</td>
</tr>
</tbody>
</table>
| 1985 | Thurs, Oct 24| 57 | none   | 93.4
| 1991 | Thurs, Oct 24| 113| numerous| 12-page "Appointments" section, 15 full pages of ads, including |

<table>
<thead>
<tr>
<th>Year</th>
<th>Date</th>
<th>Pages</th>
<th>Number</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1985</td>
<td>Fri, Oct 24</td>
<td>126</td>
<td>11</td>
<td>92.0</td>
</tr>
<tr>
<td>1975</td>
<td>Fri, Oct 24</td>
<td>113</td>
<td>41</td>
<td>73.4 Late London edition</td>
</tr>
<tr>
<td>1965</td>
<td>Mon, Oct 24</td>
<td>62.5</td>
<td>78</td>
<td>150.0 Royal edition</td>
</tr>
<tr>
<td>1955</td>
<td>Sun, Oct 24</td>
<td>130</td>
<td>78</td>
<td>62.5 Royal edition</td>
</tr>
<tr>
<td>Year</td>
<td>Date</td>
<td>Employers</td>
<td>Ads from Job Seekers</td>
<td>% Ads from Employers</td>
</tr>
<tr>
<td>------</td>
<td>------------</td>
<td>-----------</td>
<td>----------------------</td>
<td>----------------------</td>
</tr>
<tr>
<td>1851</td>
<td>Fri, Oct 24</td>
<td>None</td>
<td>None</td>
<td>N/A</td>
</tr>
<tr>
<td>1861</td>
<td>Thurs, Oct 24</td>
<td>8</td>
<td>141</td>
<td>5.4</td>
</tr>
<tr>
<td>1871</td>
<td>Tues, Oct 24</td>
<td>8</td>
<td>130</td>
<td>13.2</td>
</tr>
<tr>
<td>1881</td>
<td>Mon, Oct 24</td>
<td>6</td>
<td>156</td>
<td>3.7</td>
</tr>
<tr>
<td>1891</td>
<td>Sat, Oct 24</td>
<td>6</td>
<td>66</td>
<td>13.2</td>
</tr>
<tr>
<td>1901</td>
<td>Thurs, Oct 24</td>
<td>14</td>
<td>78</td>
<td>15.2</td>
</tr>
<tr>
<td>1911</td>
<td>Tues, Oct 24</td>
<td>22</td>
<td>74</td>
<td>22.9</td>
</tr>
<tr>
<td>1921</td>
<td>Fri, Oct 24</td>
<td>219</td>
<td>94</td>
<td>70.0</td>
</tr>
<tr>
<td>1931</td>
<td>Sat, Oct 24</td>
<td>61</td>
<td>96</td>
<td>38.9</td>
</tr>
<tr>
<td>1941</td>
<td>Fri, Oct 24</td>
<td>219</td>
<td>94</td>
<td>70.0</td>
</tr>
<tr>
<td>1951</td>
<td>Wed, Oct 24</td>
<td>numerous</td>
<td>numerous</td>
<td>95.0</td>
</tr>
<tr>
<td>1961</td>
<td>Tues, Oct 24</td>
<td>numerous</td>
<td>numerous</td>
<td>88.8</td>
</tr>
<tr>
<td>1971</td>
<td>Sun, Oct 24</td>
<td>numerous</td>
<td>numerous</td>
<td>95.0</td>
</tr>
<tr>
<td>1981</td>
<td>Sat, Oct 24</td>
<td>289</td>
<td>28</td>
<td>91.2</td>
</tr>
<tr>
<td>1991</td>
<td>Thurs, Oct 24</td>
<td>686</td>
<td>11</td>
<td>98.4</td>
</tr>
<tr>
<td>2001</td>
<td>Wed, Oct 24</td>
<td>381</td>
<td>2</td>
<td>99.5</td>
</tr>
<tr>
<td>2011</td>
<td>Mon, Oct 24</td>
<td>224</td>
<td>4</td>
<td>98.2</td>
</tr>
</tbody>
</table>

This is a recession month.

The so-called “Jobless Recovery”

The national unemployment remained at 7 percent in October during the recession of 1990-1991, which ended in March.

All ads on p. 1-B2-B3, except “Help Wanted” ads posted by employers, are placed under occupational categories.

% is approximate.
Figure 1: The London Times 1815-1991

Figure 2: The New York Times 1861-2011
Note: Graph shows welfare as a function of $c_p$, for $n = m = 1$, $u_W = u_F = 100$, $u_0 = 0$, $\alpha = 0.7$.

Note: Graph shows welfare as a function of $\alpha$, for $n = m = 1$, $u_W = u_F = 100$, $c_p = 20$, $u_0 = 0$. 