

## Lecture 7: Life Tables

### Definitions

$x$  = Age interval

$w$  = Maximum age-class

$n_x$  = Number of individuals alive at start of age  $x$

$l_x$  = Percentage of individuals still alive at start of age  $x$

$m_x$  = number of female offspring per female of age  $x$

$p_x$  = Age-specific survival rate from age  $x$  to age  $x+1$

### Basic calculations

$$l_x = \frac{n_x}{n_0} \quad p_x = \frac{l_{x+1}}{l_x} = \frac{n_{x+1}}{n_x}$$

### Life-table calculations

Gross reproductive rate:  $GRR = \sum_{x=0}^w m_x$

The net reproductive rate ( $R_0$ ) is the average number of female offspring per female per generation. Usually assumes a 1:1 sex ratio at birth. Indicates population status: increasing ( $R_0 > 1$ ) or decreasing ( $R_0 < 1$ ).

Net reproductive rate:  $R_0 = \sum_{x=0}^w l_x m_x$

Generation time ( $T$ ) is the number of time units it takes an average female to produce one female offspring. The numerator is divided by  $R_0$  to control for whether the population is increasing or decreasing.

Generation time:  $T = \frac{\sum_{x=0}^w x l_x m_x}{R_0}$

The intrinsic rate of population growth ( $r$ ) is interchangeable with the finite rate of population growth ( $\lambda$ ). Population growth is stationary if  $r = 0$  and if  $\lambda = 1$ . The two metrics can be converted as:  $\lambda = e^r$  and  $r = \ln \lambda$ . Calculations of  $r$  based on the below equation assume a stable age distribution and a stationary population size.

$$r = \frac{\ln R_0}{T}$$

The Euler equation is an improved method for estimation of  $r$  from life-table data. It is not an analytical solution because  $r$  cannot be isolated by algebra and iteration must be used to solve for  $r$ .

$$1 = \sum_{x=0}^w l_x m_x e^{-rx}$$

## Age-specific Life History Parameters

Life expectancy ( $E_x$ ) is if an individual has survived to a particular age-class, what is the expected number of time units they will survive in the future. If juvenile mortality is high, life expectancy may be greatest for individuals of intermediate age.

$$E_x = \frac{\sum_{y=x}^w l_y}{l_x}$$

Reproductive value ( $v_x$ ) is the age-specific expectation of future offspring, and is measured in units of female offspring per female. For a stable population at equilibrium:

$$v_x = \sum_{y=x}^w \frac{l_y}{l_x} m_x$$

Reproductive values are then usually scaled by dividing each  $v_x$  value by the reproductive value of the youngest age-class ( $v_0$ ). One of the greatest insights of evolutionary ecology is that reproductive value can be partitioned into current vs. future reproduction:

$$v_x = m_x + \sum_{y=x+1}^w \frac{l_y}{l_x} m_x$$

In applied ecology, management activities are often targeted at age-classes with high reproductive value. Conservation biologists might protect those age-classes in a declining population, whereas wildlife managers might target those age-classes for fertility control in pest species.